

# Coherent Synchrotron Radiation Studies and Applications at the NSLS

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*Brookhaven National Laboratory*

*in collaboration with*

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C.-C. Kao, S.L. Kramer, B. Podobedov, J.B. Murphy & X.-J. Wang

*NSLS / Brookhaven National Laboratory*

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*UVSOR Workshop on Terahertz Coherent Synchrotron Radiation*

*Inst. for Molecular Science, Nat'l Inst. of Nat. Science, Okazaki, Sept. 23-25, 2007*

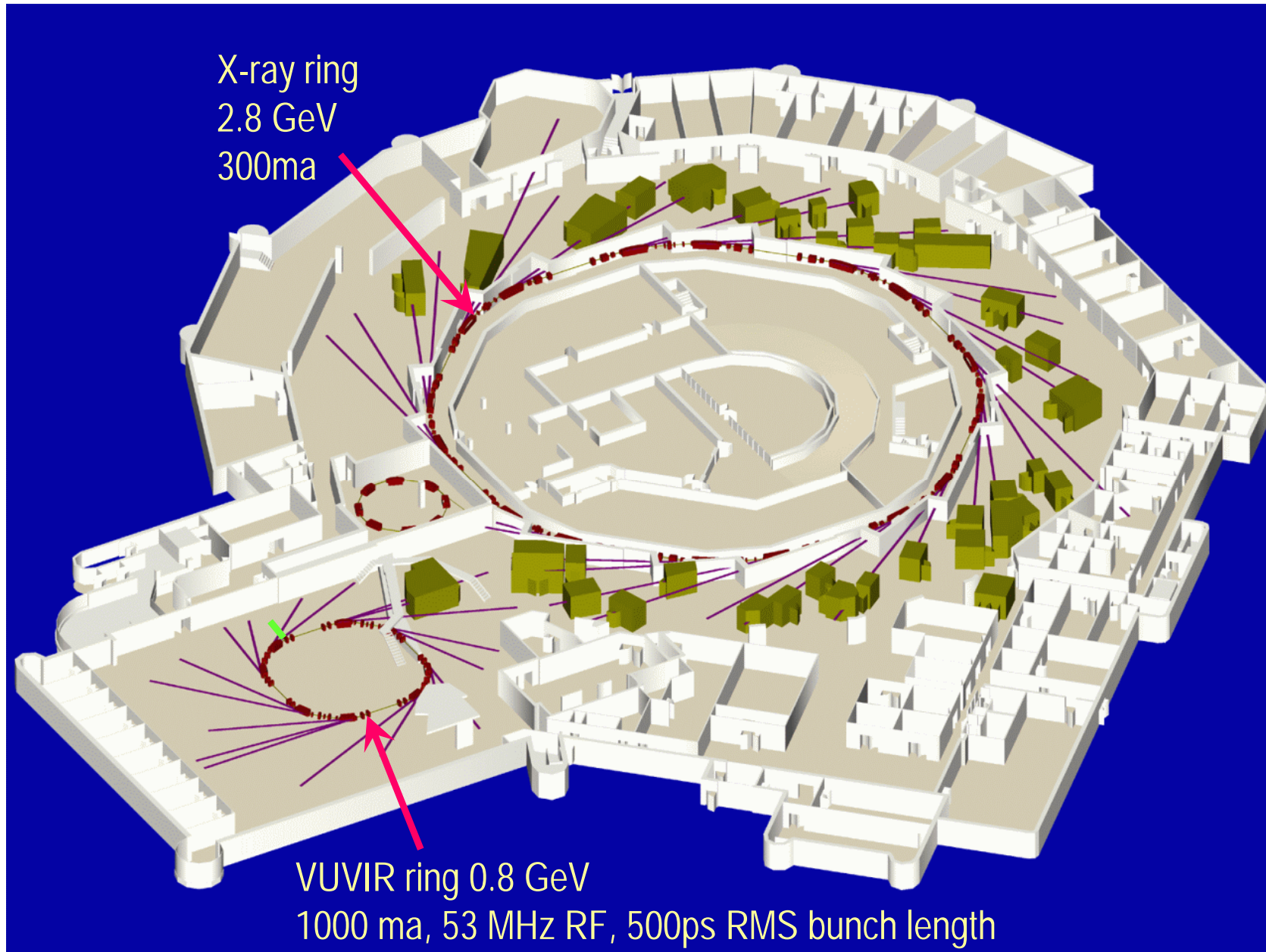
- Coherent synchrotron radiation from the NSLS VUV/IR storage ring:
  - Far-infrared spectroscopy at beamline U12IR
  - CSR bursts in the  $\sim 100$  GHz spectral range.
- Coherent transition radiation from the NSLS Source Development Laboratory linac:
  - large THz radiation pulses.
  - electro-optic measurement setup to sense waveforms/fields
  - issues when fields are large (time-dependence)
  - non-linear optics application:  
phase modulation to control spectral content, chirping, etc.
- Potential application:
  - switching behavior in ferroelectrics, ferromagnets, superconductors.

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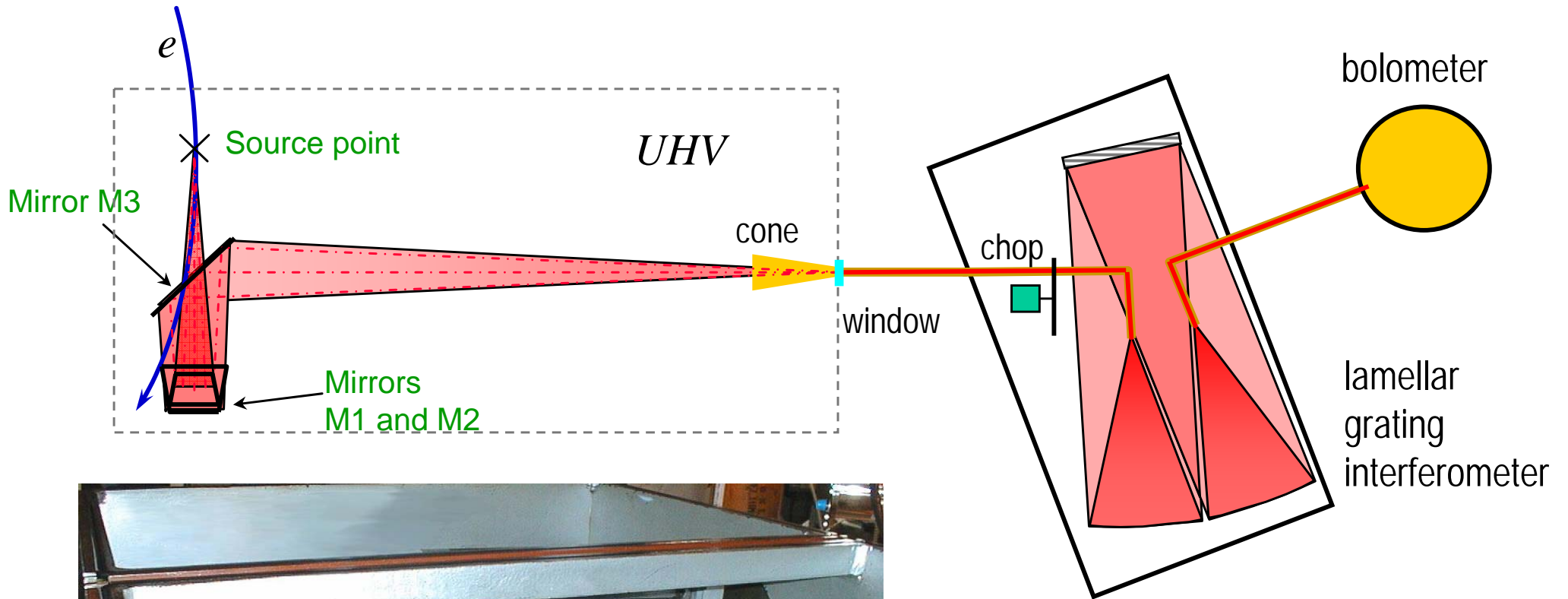
# Coherent Synchrotron Radiation (CSR)

- 1st observations in linacs:
  - Nakazato et al (PRL '89), Happek et al (PRL '91)
- As a linac bunch diagnostic:
  - Shibata et al (PRE '94), Lai et al (PRE '94), Yan et al (PRL '00)
- As a THz source
  - Ishi et al (PRA '91), Takahashi et al (RSI '98), Carr et al., (Nature '02)
- CSR also from storage rings
  - Arpe et al, Carr et al, Anderson et al, Abo-Bakr et al., ALS, SPRing-8, MIT/Bates, ...

# NSLS Storage Rings

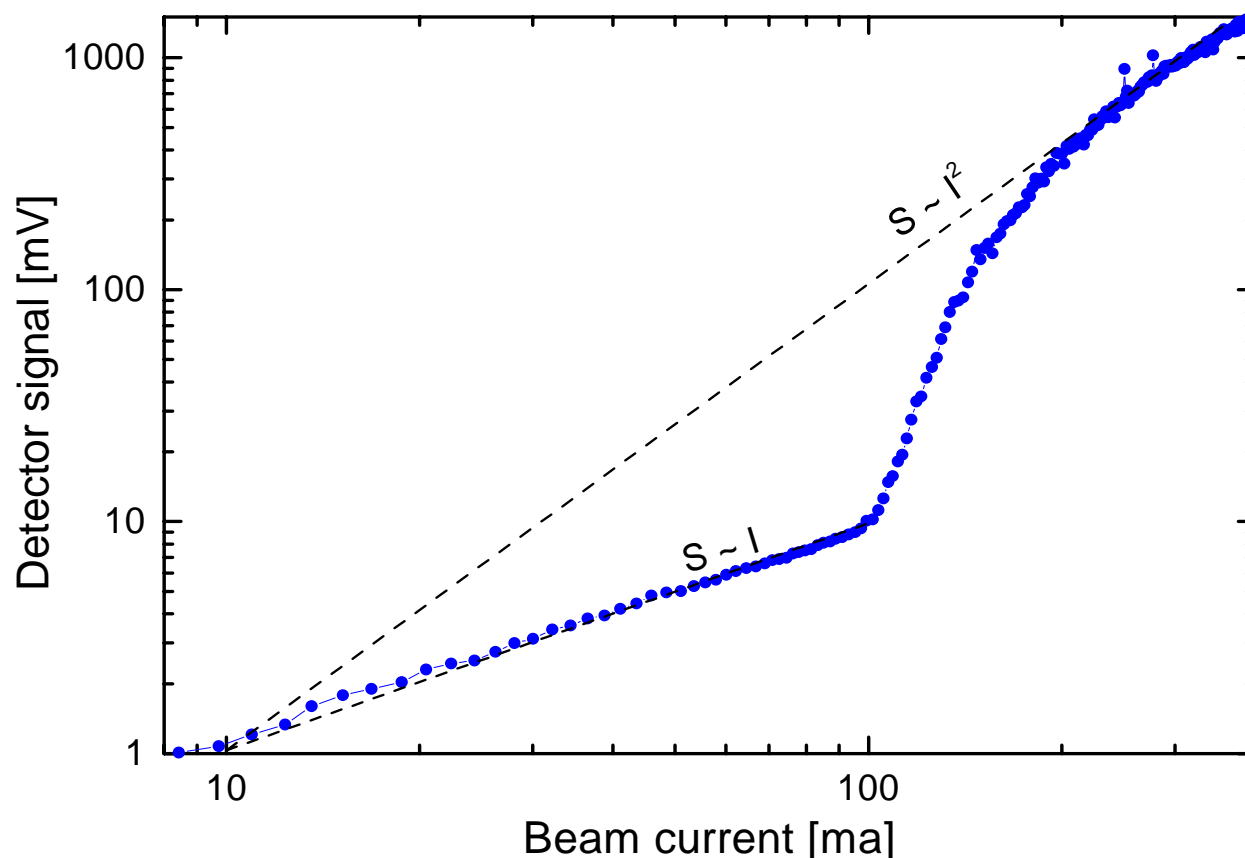


# U12IR - beamline / spectrometer

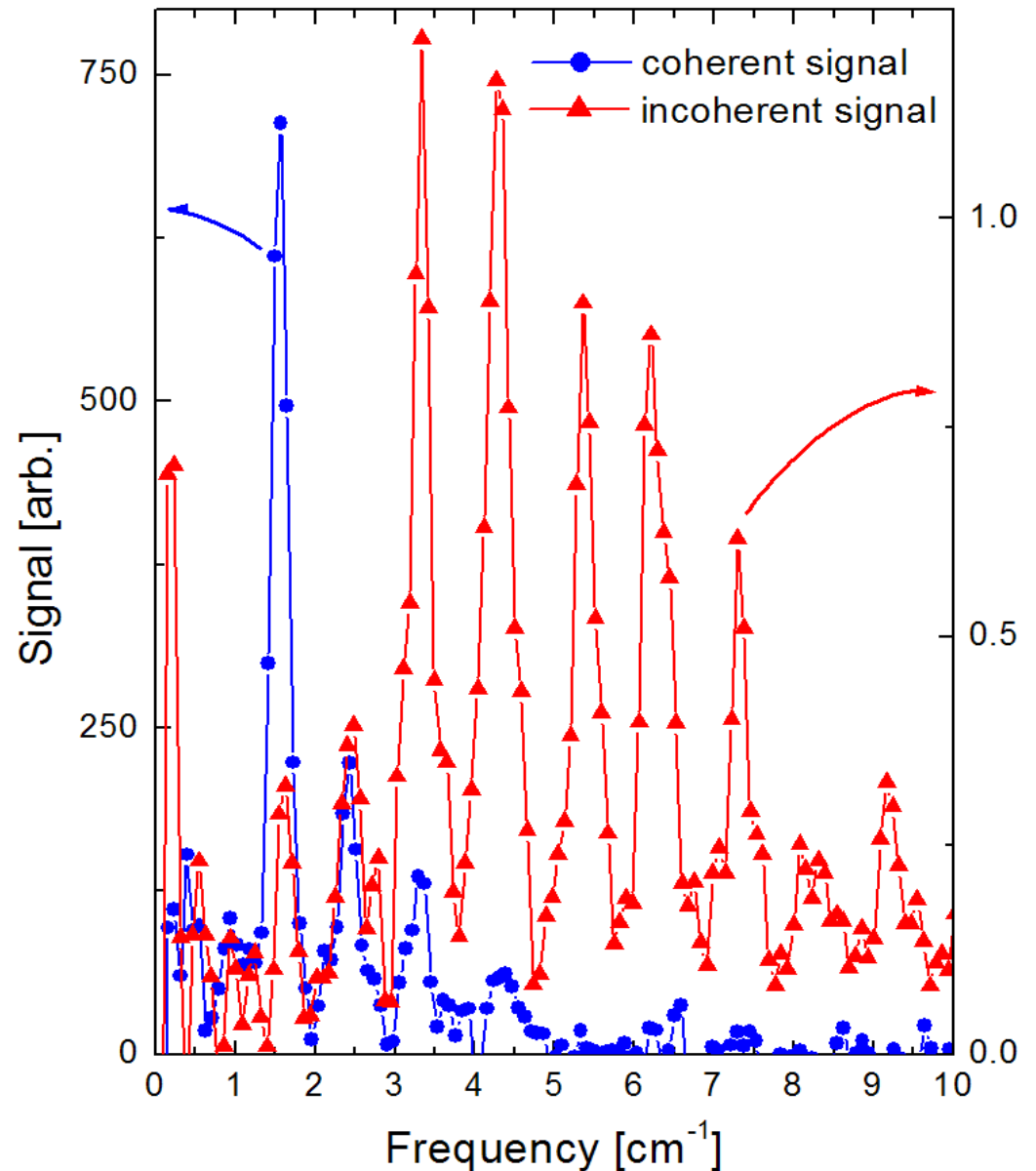
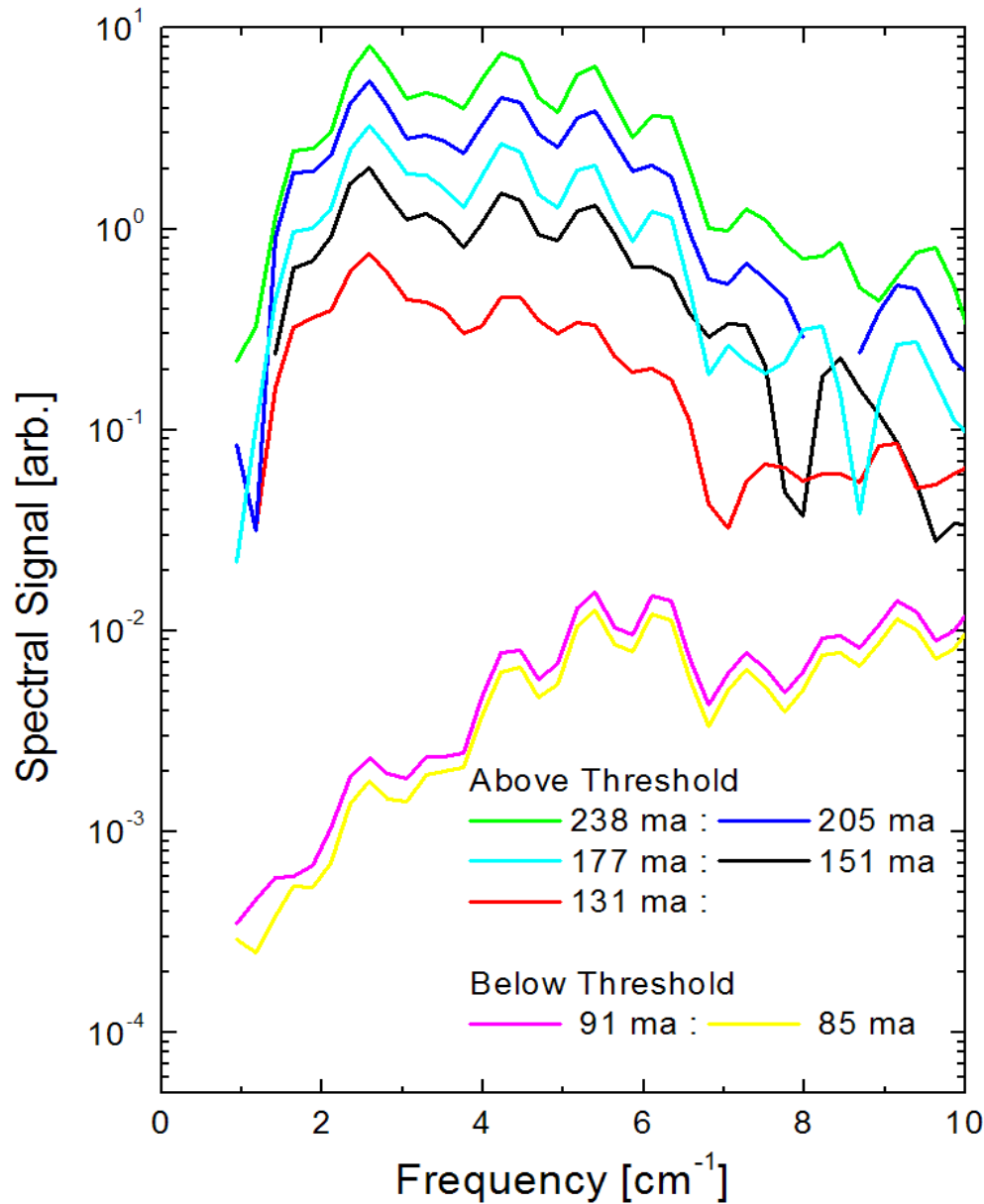


# Coherent synchrotron radiation: Beam current dependence

- First observed: October 1997.
- $I^2$  dependence beyond threshold.
- threshold depends on operating parameters (E, bunch stretching,  $\alpha$ ).
  - G.L. Carr et al, PAC-99, SPIE: vol. **3775** p.88 (1999),  
*Nucl. Instrum. & Meth. Phys. Res. A* **463**, 387 (2001)



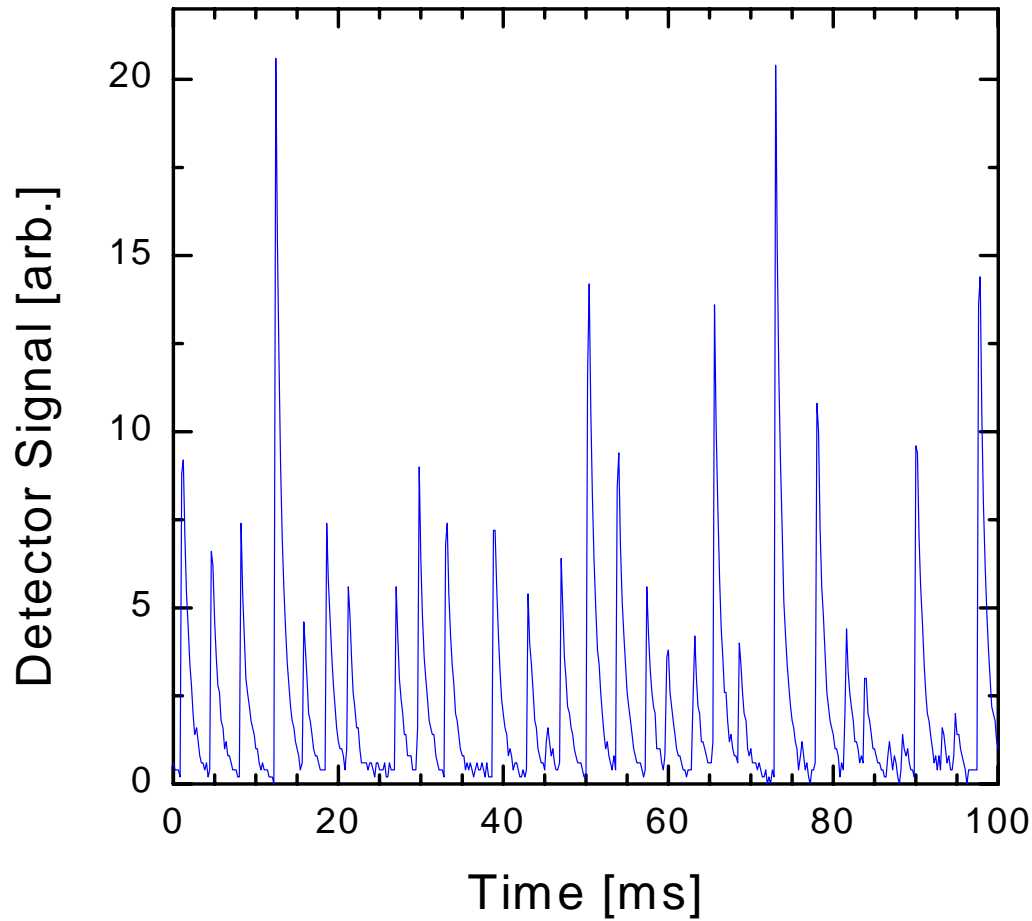
# VUV Ring Coherent SR: Relative Spectral Intensity



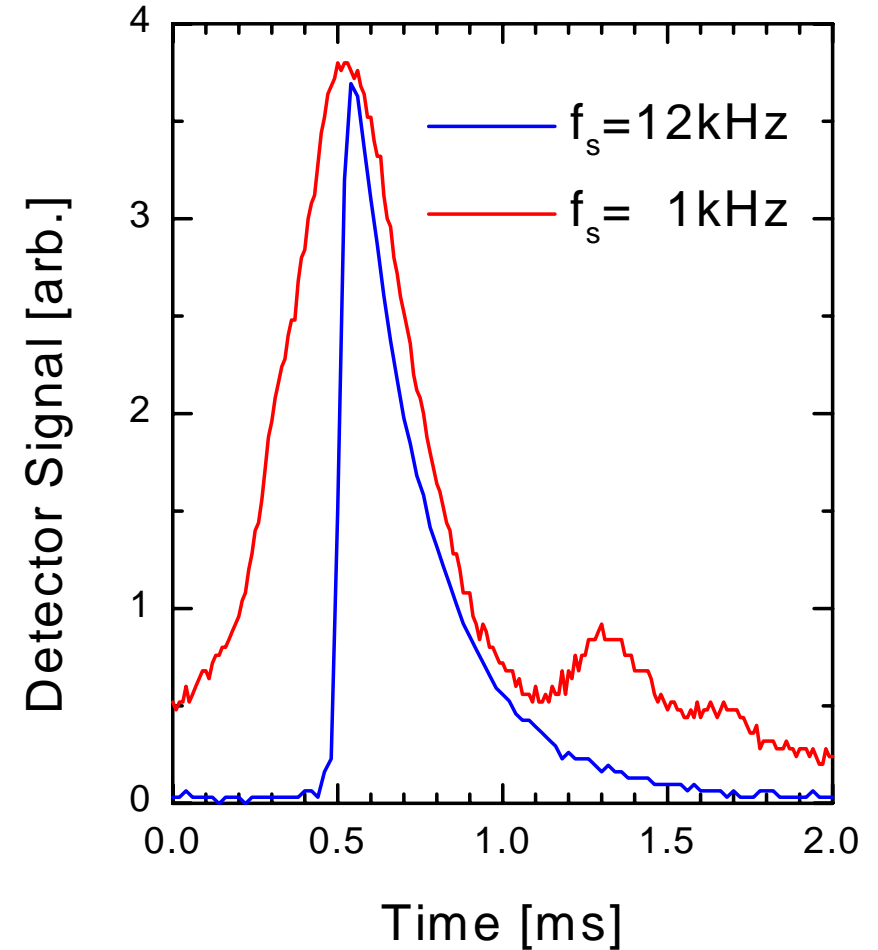


# CSR Emission Bursts

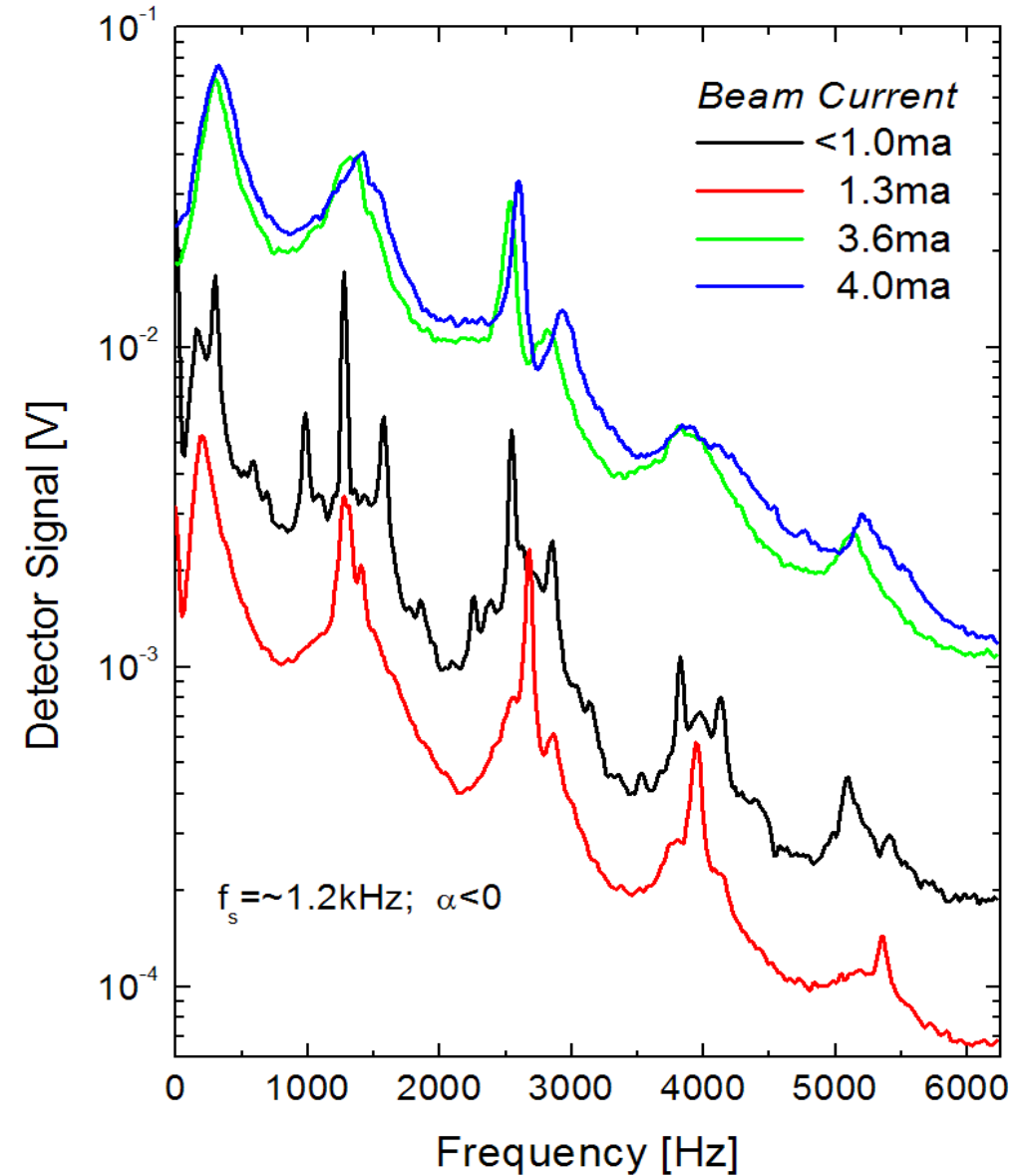
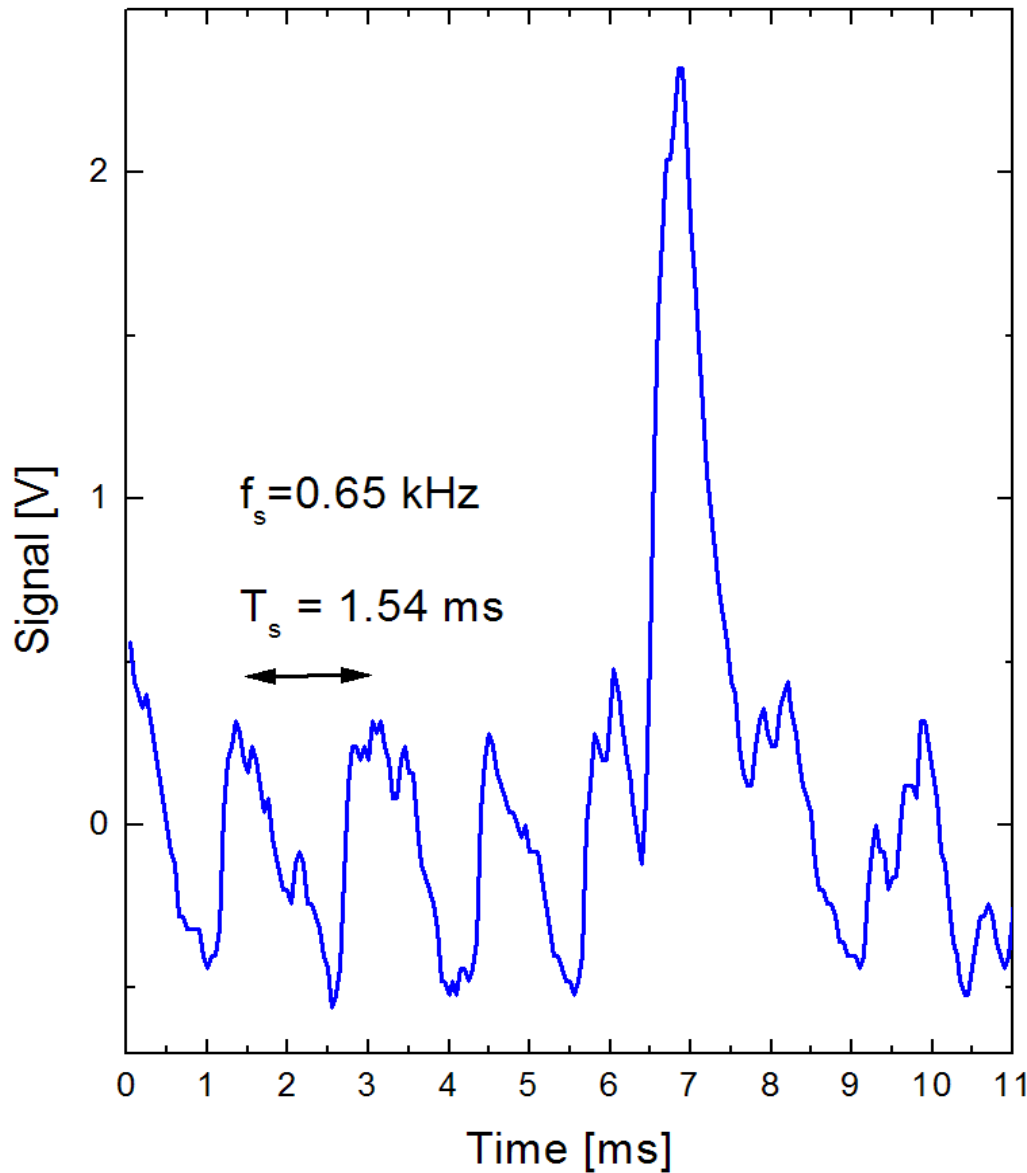
- *Quasi-periodic bursts*
- *$T \sim 1$  to  $10$  ms*
- *detector-limited fall time*



- *Risetime  $< 100 \mu\text{s}$  for  $\alpha = \alpha_0$*
- *increases with decreasing  $\alpha$*

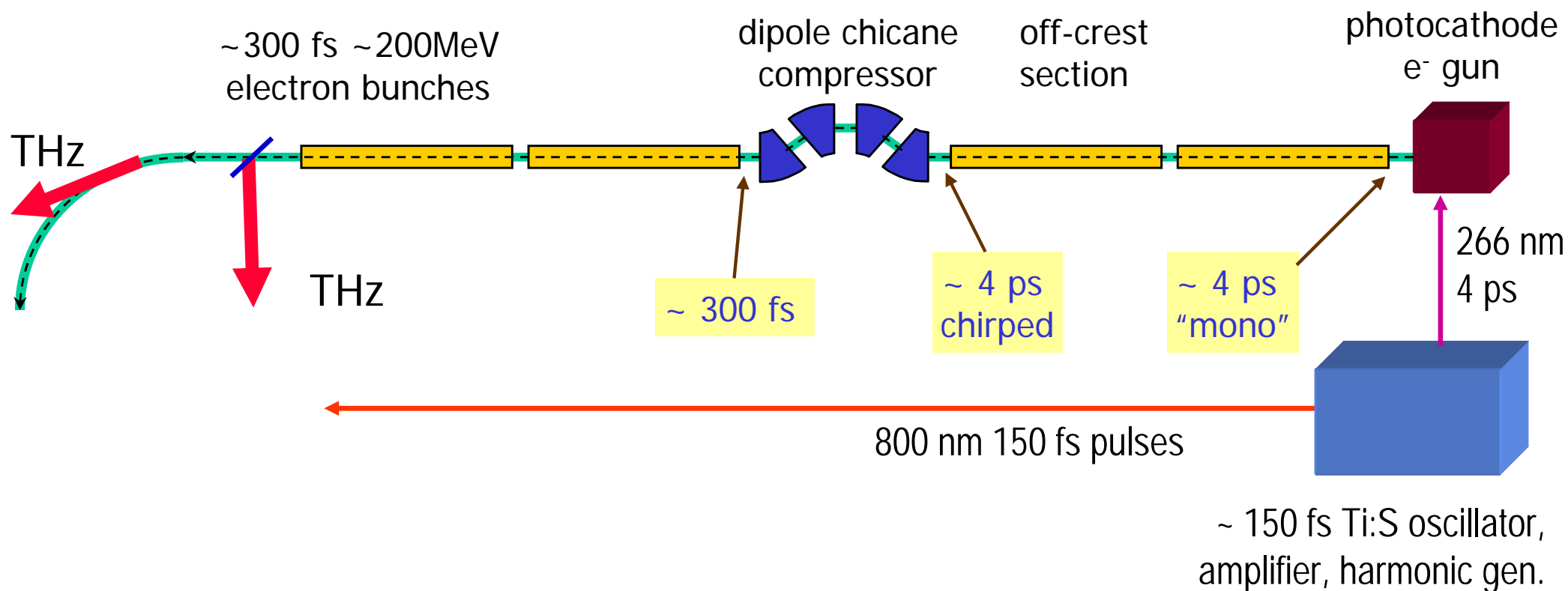


# Coherent Bursts: Time Structure (spectrum analysis)



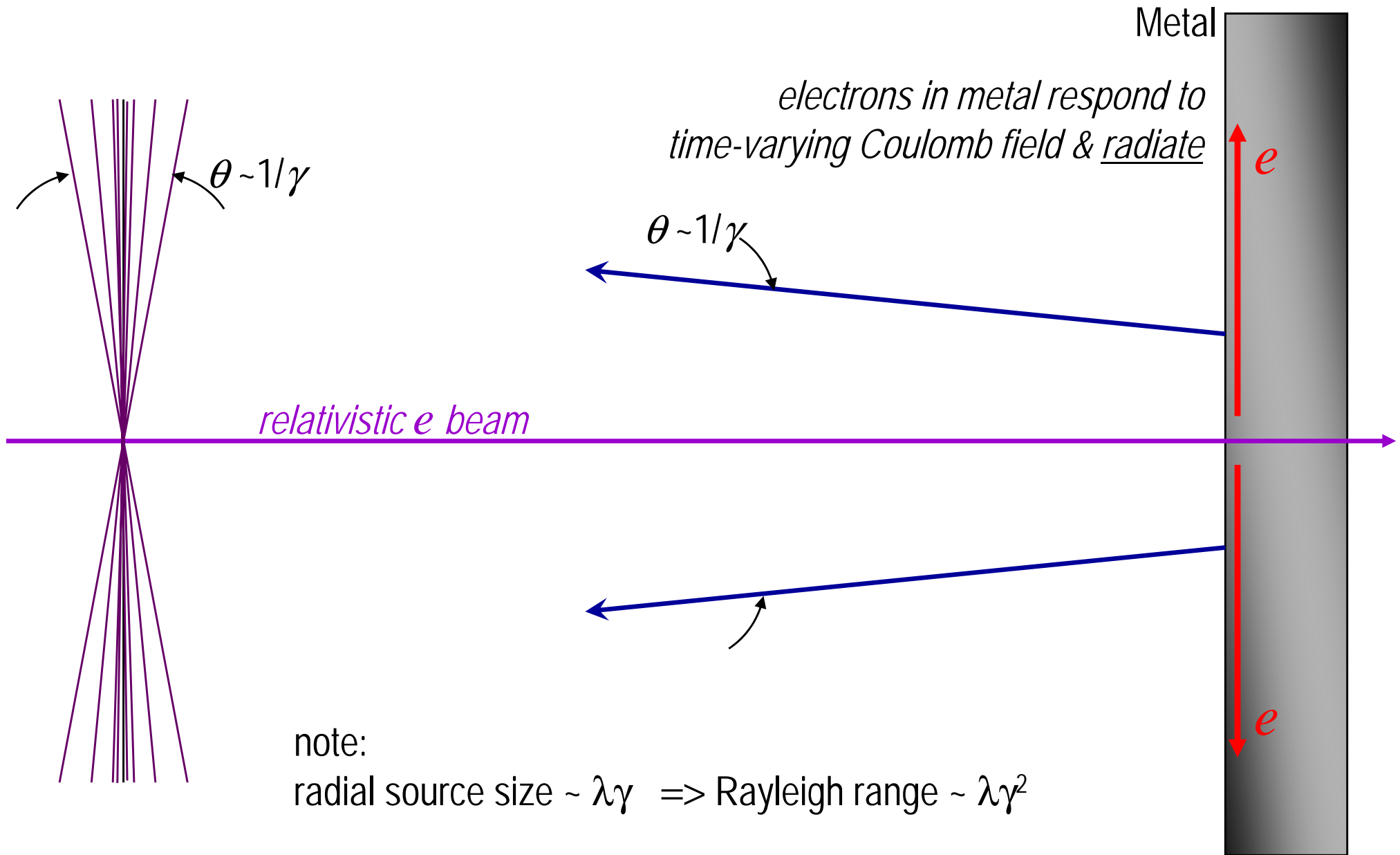
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phase modulation to control spectral content, chirping, etc.
- Potential application:
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- ◆ Photocathode gun produces  $\sim 0.84\text{nC}$  ( $5 \times 10^9$  electrons) per “shot”



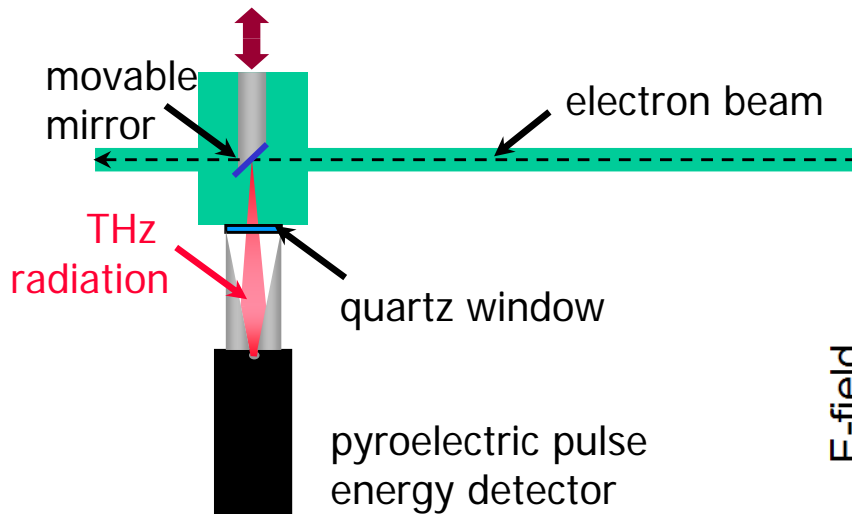
- ◆ Coherent output to over 1 THz. Potential for shorter bunches with less charge.
- ◆ Low rep. rate (1 to 10 Hz)

# Transition Radiation from Relativistic Electrons



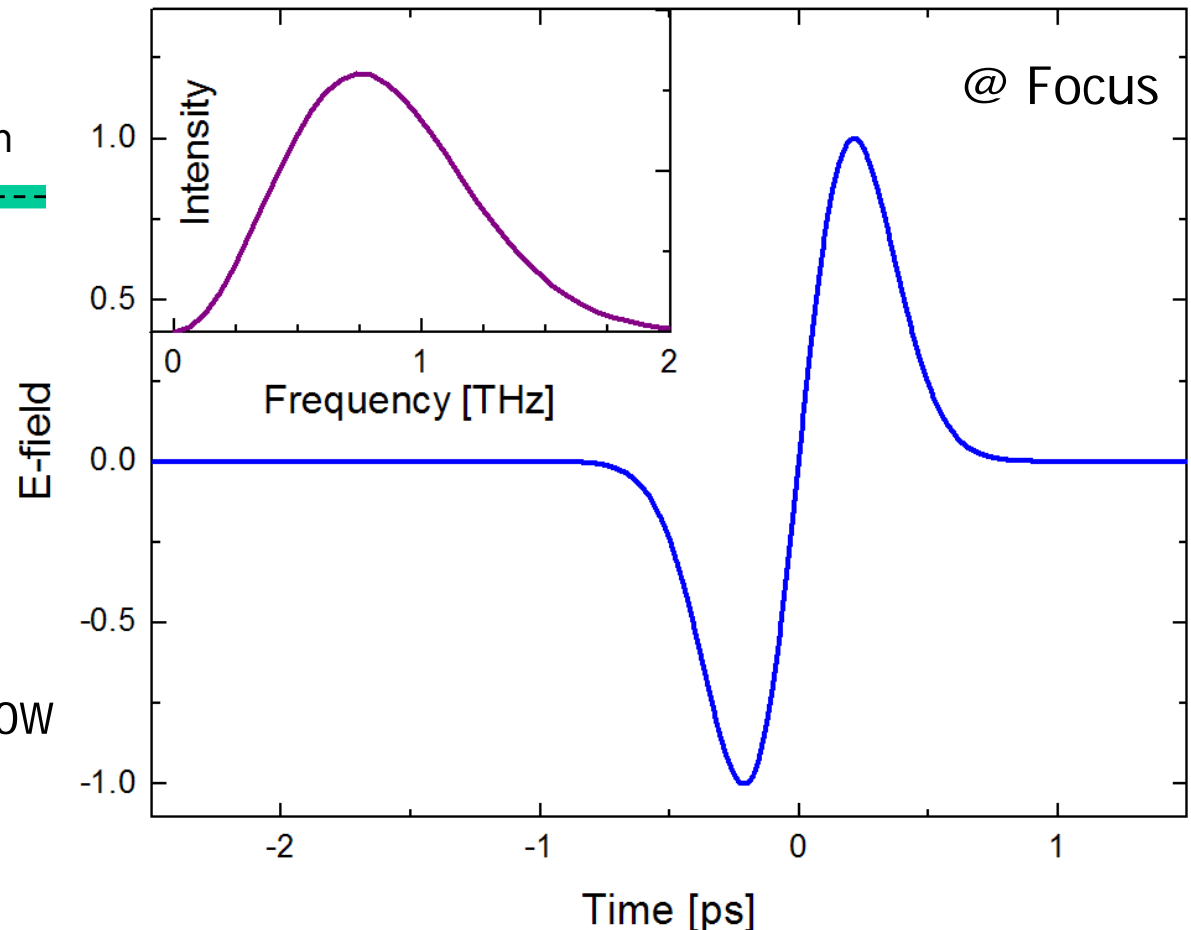
# Coherent THz Pulses

Transition Radiation: Energy per electron per  $\omega \rightarrow E = \frac{e^2}{\pi c} \left[ \ln\left(\frac{2}{1-\beta}\right) - 1 \right]$   
 $10^{10}$  electrons, 116 MeV coherent to 1 THz  
 => pulse energy of 400  $\mu\text{J}$   
*(Happek et al, PRL)*



Finite source and aperture, quartz window reflection => ~ 35% efficient or 140  $\mu\text{J}$ .  
 We have measured 100  $\mu\text{J}$  per pulse.

*Expected behavior*

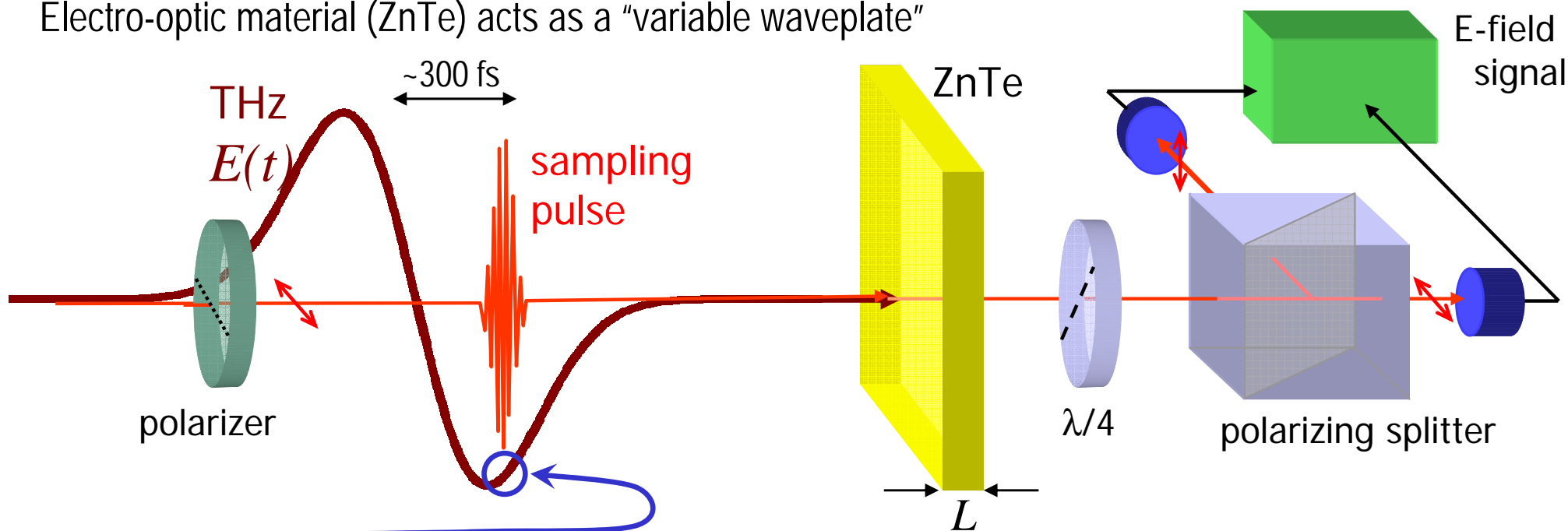


# THz Characterization: Electro-Optic Methods

Coherent detection setup for measuring THz waveforms using Pockels Effect: "THz Electro-Optic switch"  
*(Zhang et al, Heinz et al)*

$$E_{laser} \sim \cos \left[ \left( \frac{2\pi n}{\lambda_0} \right) z - \omega_0 t + \Delta\phi_E(t) \right] \text{ where } \Delta\phi_E(t) = \left( \frac{2\pi L}{\lambda_0} \right) \Delta n[E_{THz}(t)]$$

Electro-optic material (ZnTe) acts as a "variable waveplate"



$$E(t) = E(t_0) + \frac{dE}{dt}(t-t_0) + \frac{1}{2} \frac{d^2E}{dt^2}(t-t_0)^2 + \dots$$

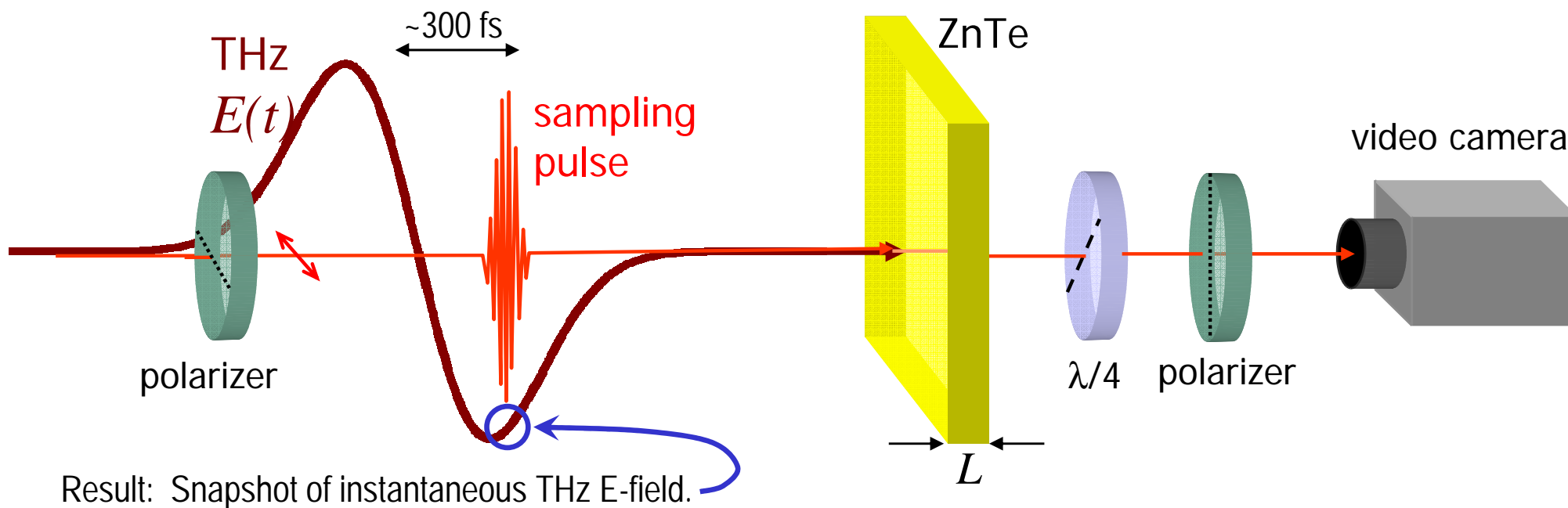
Result: Detector signal gives instantaneous THz E-field.

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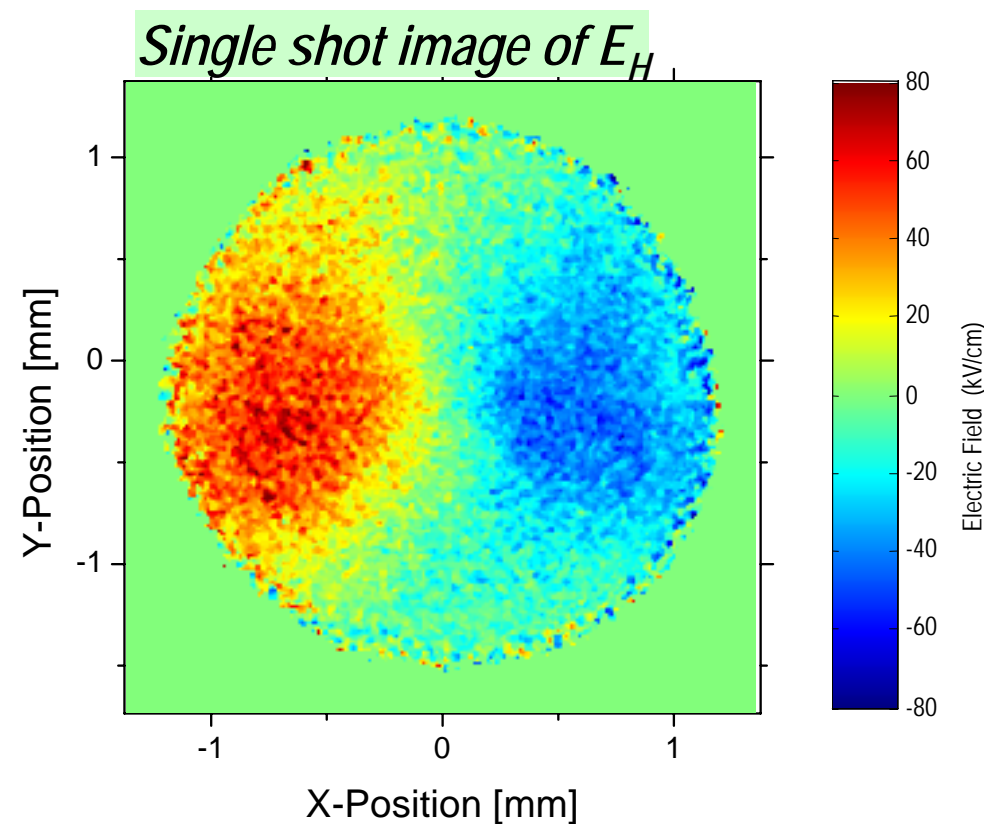
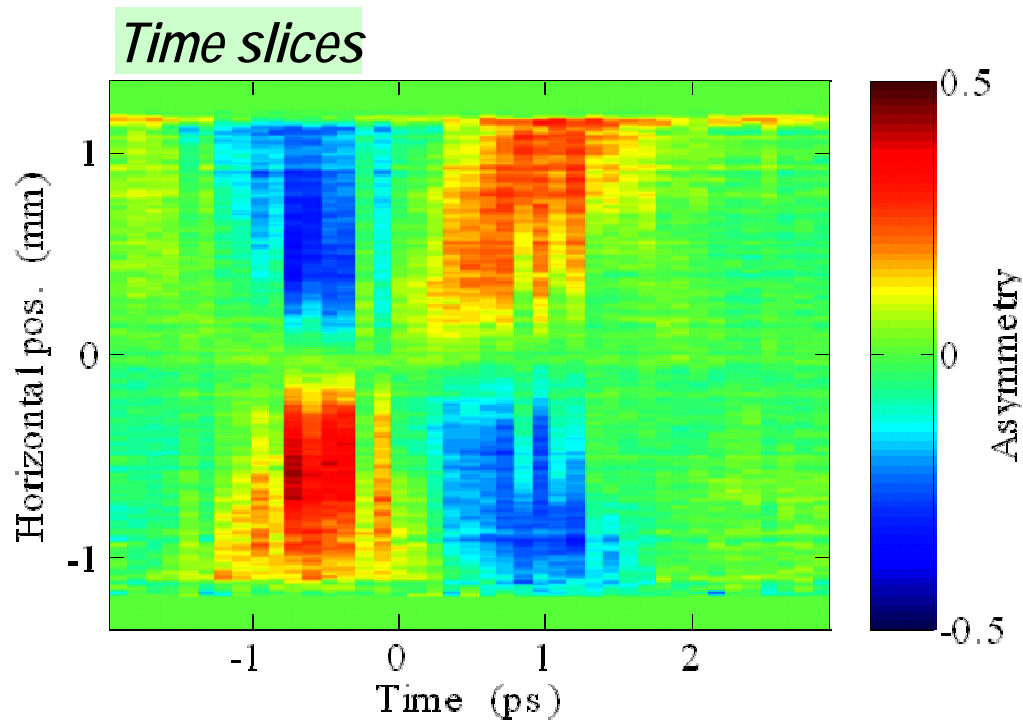


*Low charge (intensity) measurement:*

*Single-cycle at focus: note that Transition Radiation is radially polarized*

*Jitter (~ 150 fs) limits ability to extract detailed waveforms & spectra.*

*Need a "single-shot" method*



# Single-Shot Electro-Optic Method

Use chirped sampling laser to encode waveform's entire time-dependence onto different wavelengths of laser in a single pulse. Avoids need for multiple sampling.  
 [Jiang and Zhang, *Appl. Phys. Lett.* **72**, 1945 (1998)].

$$E_{laser}(x, t) = E_0 \exp[i(kx - \omega t)] = E_0 \exp[i\phi(x, t)]$$

$$\omega_{inst} \equiv -\partial\phi(x, t)/\partial t$$

so, if  $\phi(x, t) = kx - \omega t - \beta t^2$  then  $\omega_{inst} = \omega + \beta t \rightarrow$  linear chirp

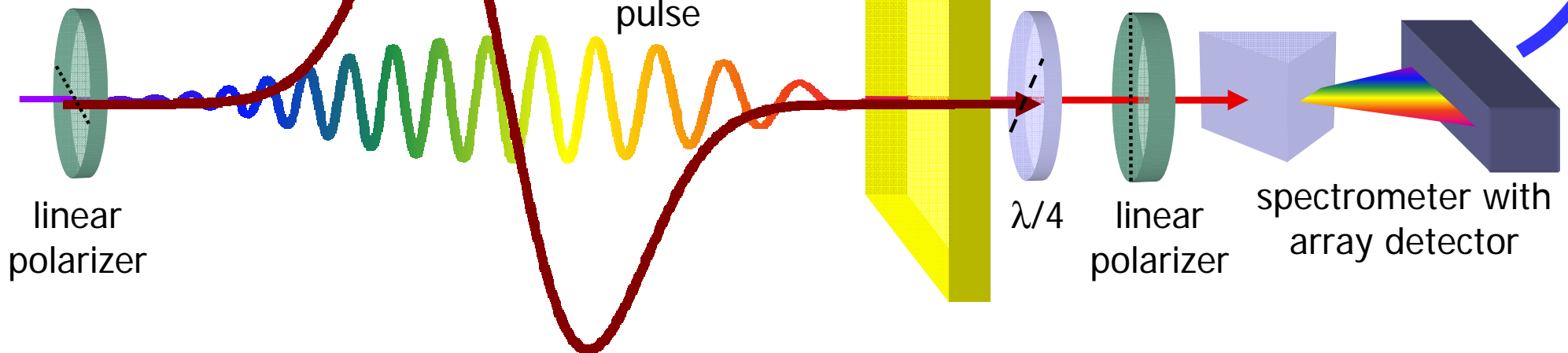
Setup for single-shot  
EO sensing of  
THz waveform

THz

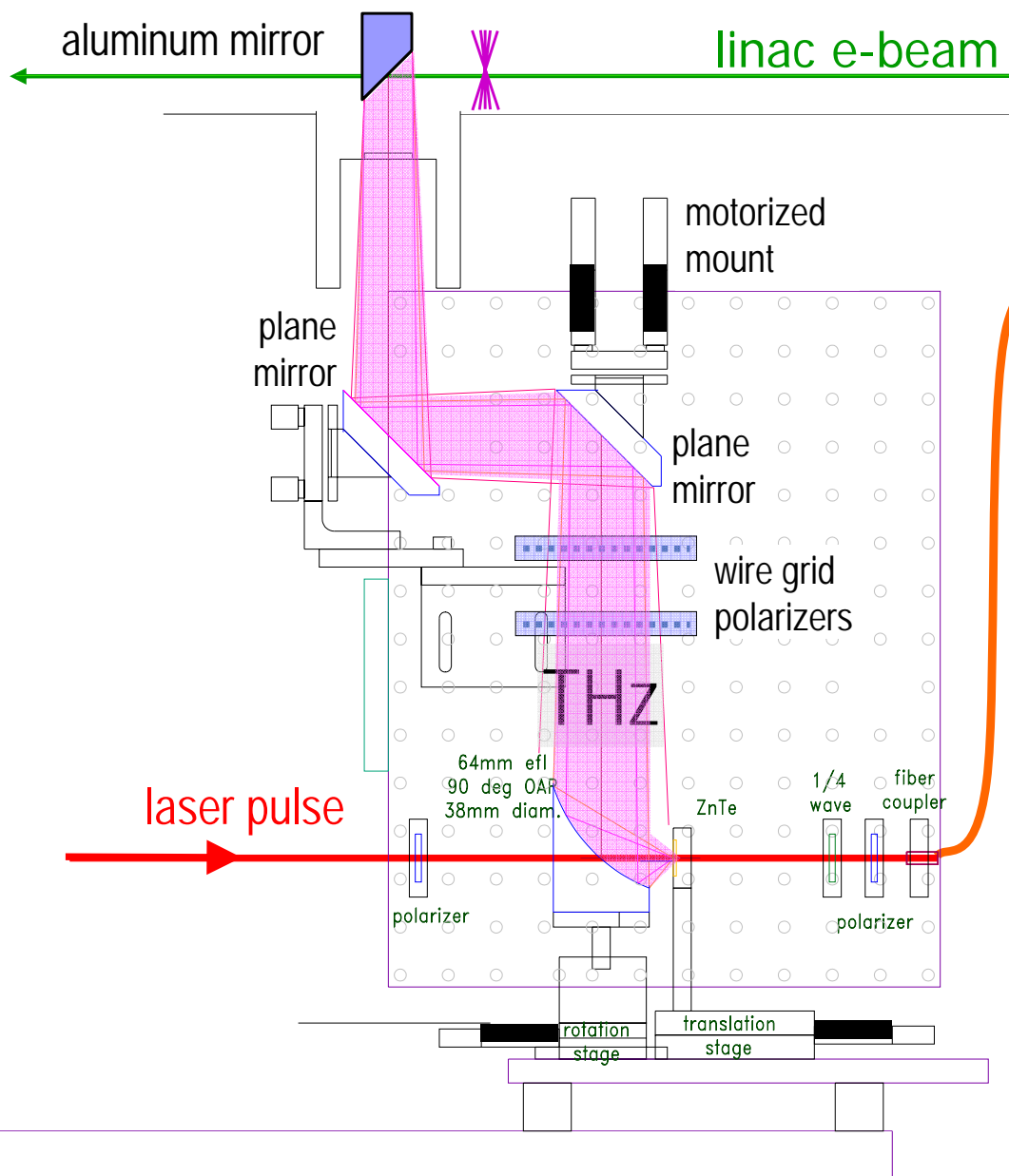
chirped  
sampling  
pulse

ZnTe

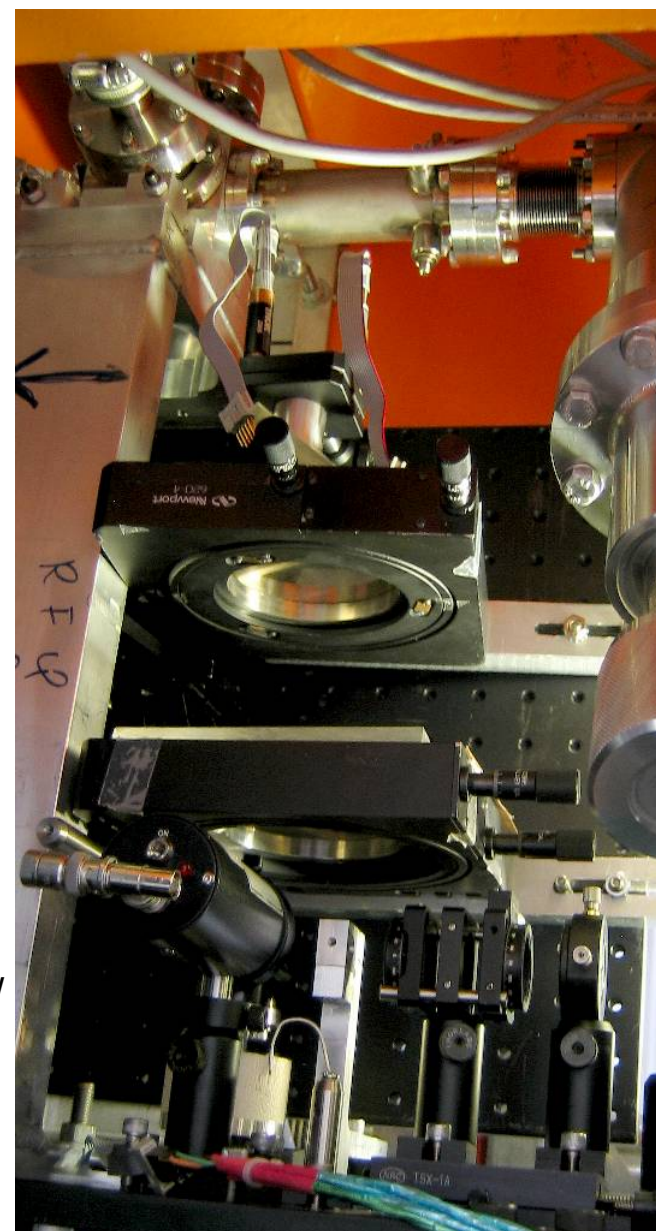
Wavelength | Time



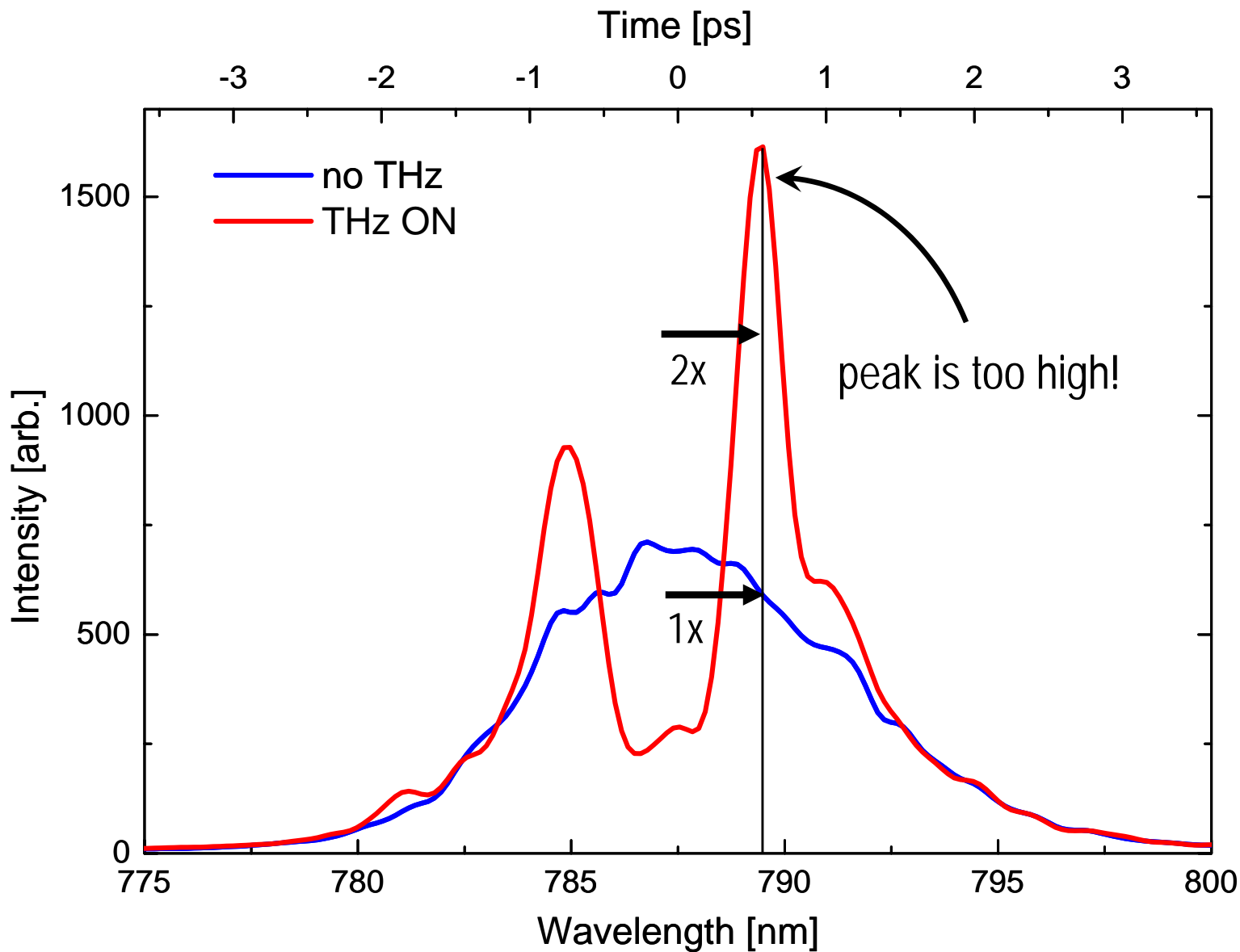
# Layout for Characterizing THz Waveforms



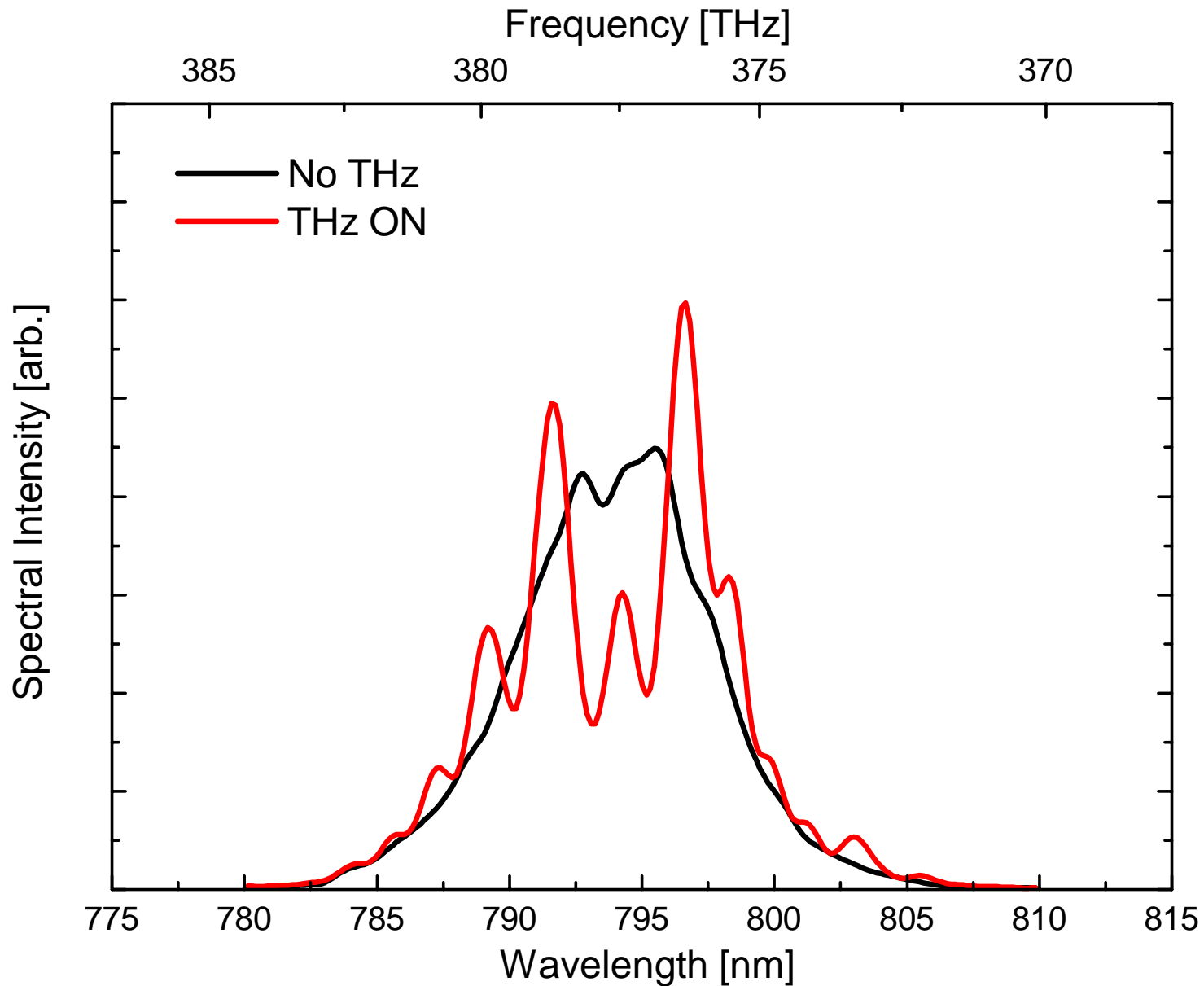
Fiber coupled spectrometer



# Single-Shot EO Sampling of SDL THz Pulse using Chirped Laser



# Single-Shot EO Sampling of SDL THz Pulse: Higher intensity

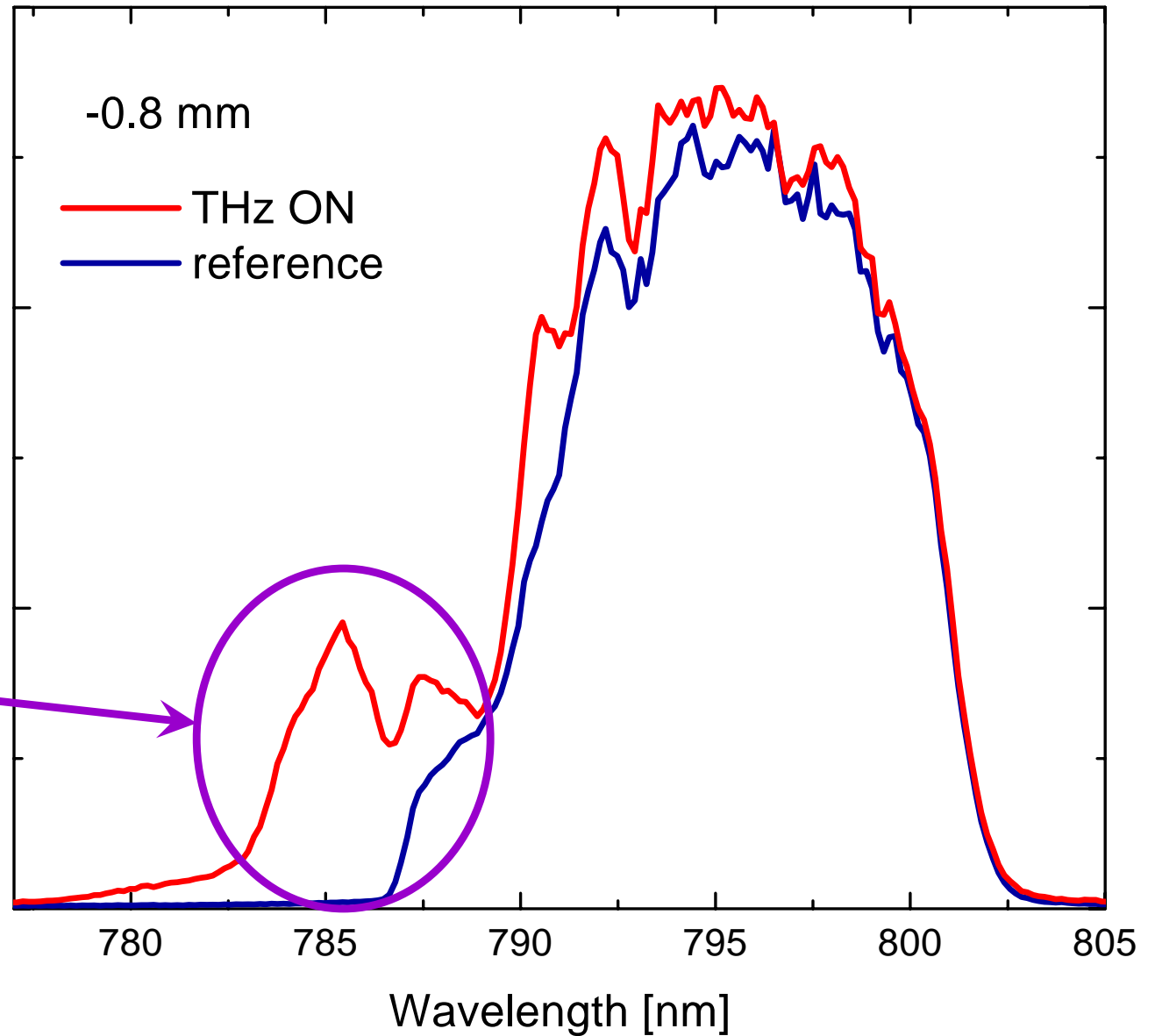


# Spectral Distribution

Now, shift relative timing between the THz and chirped laser pulse by 0.8mm (places THz nearer to the short wavelength end of the chirped laser's spectrum).

"New" spectral intensity appears in the sampling laser.

Spectral Intensity [arb.]



# Time-Dependent THz E-field and Phase Modulation Effects

- Return to details of Pockels electro-optic effect in terms of the induced phase  $\phi[E_{THz}(t)]$  for the sampling laser:

$$E_{laser} \sim \cos[\phi_0 + \phi(t)]; \quad \phi(t) = \frac{2\pi L}{\lambda_0} n[E_{THz}(t)] - \omega t$$

- Return to Taylor series expansion (this time for phase):

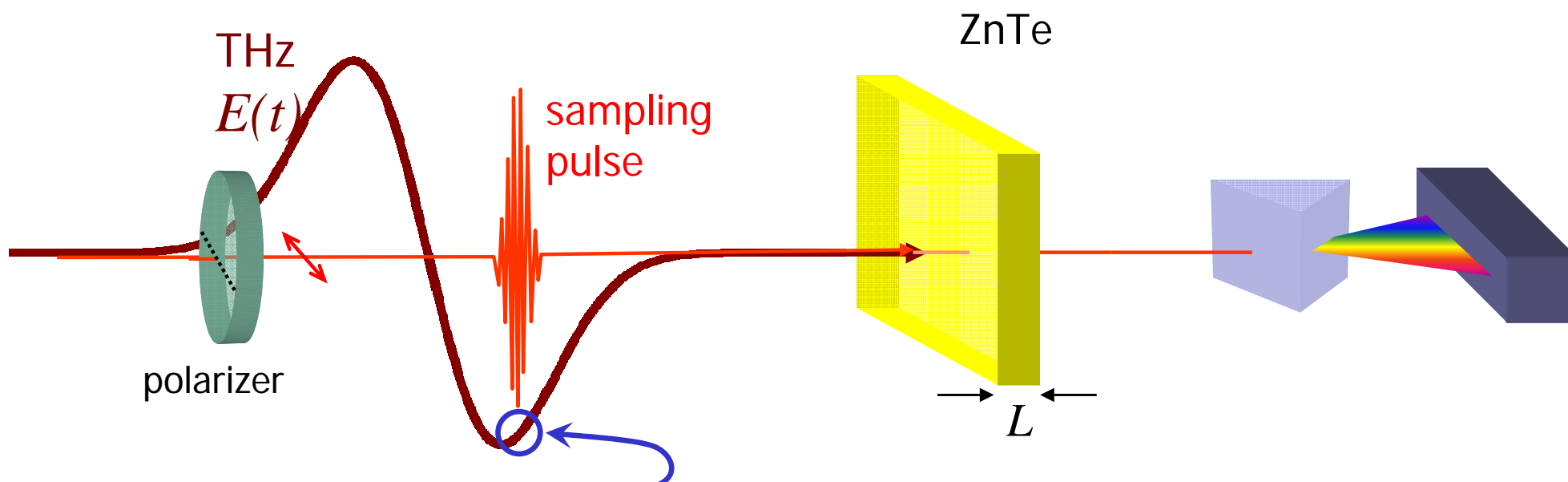
$$\phi(t) = \underbrace{\eta E(0)}_{\text{conventional EO effect}} + \underbrace{\left[ \eta \left( \frac{dE_{THz}}{dt} \right) - \omega \right]}_{\text{freq. shift}} t + \underbrace{\left[ \eta \left( \frac{d^2 E_{THz}}{dt^2} \right) \right]}_{\text{linear chirp}} t^2 + \dots \quad \text{where} \quad \eta = \frac{2}{1 + \sqrt{\epsilon}} \frac{2\pi L}{\lambda_0} n_0^3 r_{41}$$

- Different terms in phase correspond to simple phase shifts, spectral shifts and even spectral chirping.
- Result: When THz is sufficiently strong, it modifies the spectral content of the Ti:S laser.
- Note: for 1% wavelength shift at  $\lambda=800\text{nm}$  with 0.5mm ZnTe, need  $dE/dt = 1.3 \text{ MV/cm/ps}$
- Application: THz *control* of ultra-fast laser pulses (tuning, chirp+compression, lensing, ...)
- Effects simplified using an unchirped laser (to sample just a small segment of THz waveform).

"Simple" EO setup to observe time-dependent phase modulation

$$E_{laser} \sim \cos [kz + \Delta\phi_E(t) - \omega t] \quad \text{where} \quad \Delta\phi_E(t) = \left( \frac{2\pi L}{\lambda_0} \right) \Delta n[E_{THz}(t)]$$

Electro-optic material (ZnTe) acts cross phase modulator

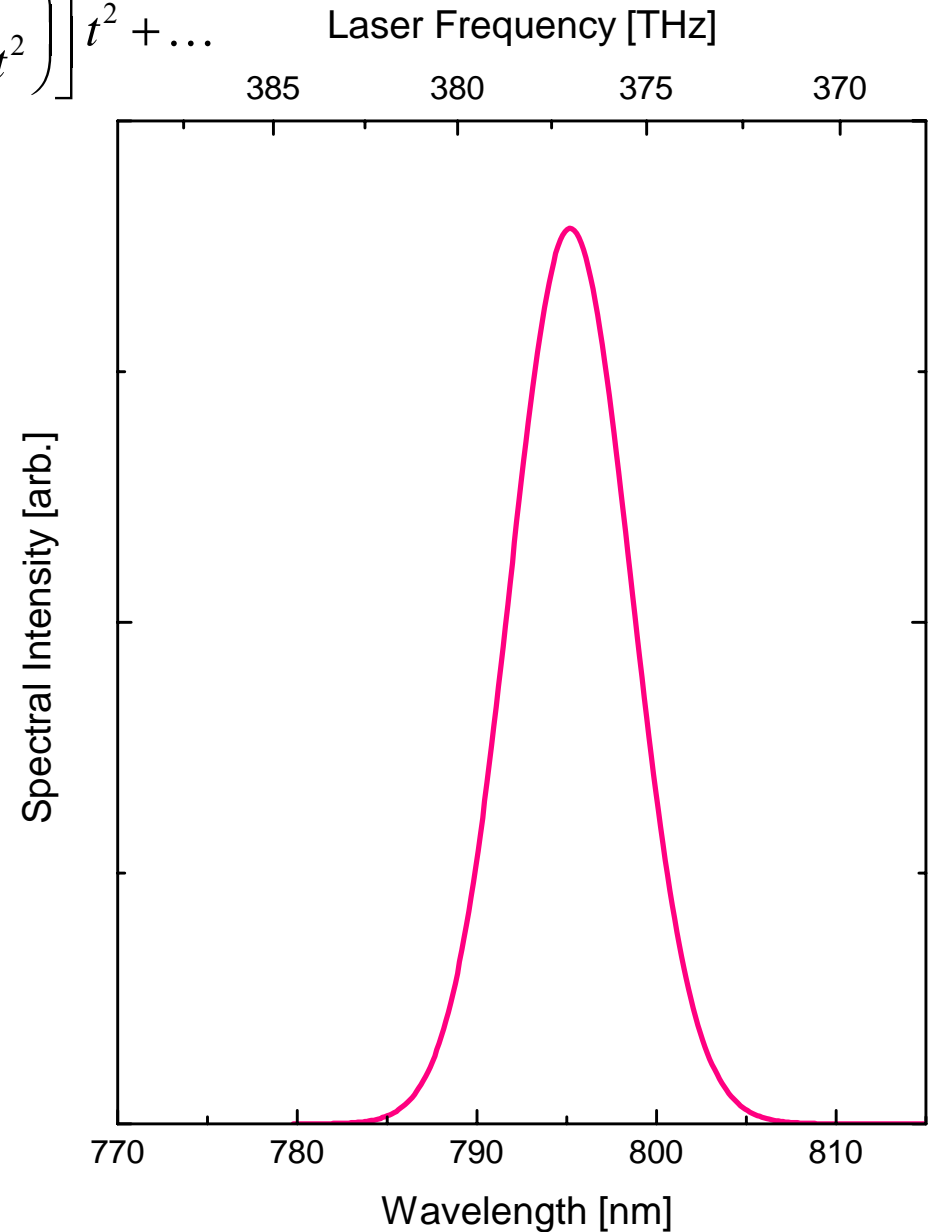
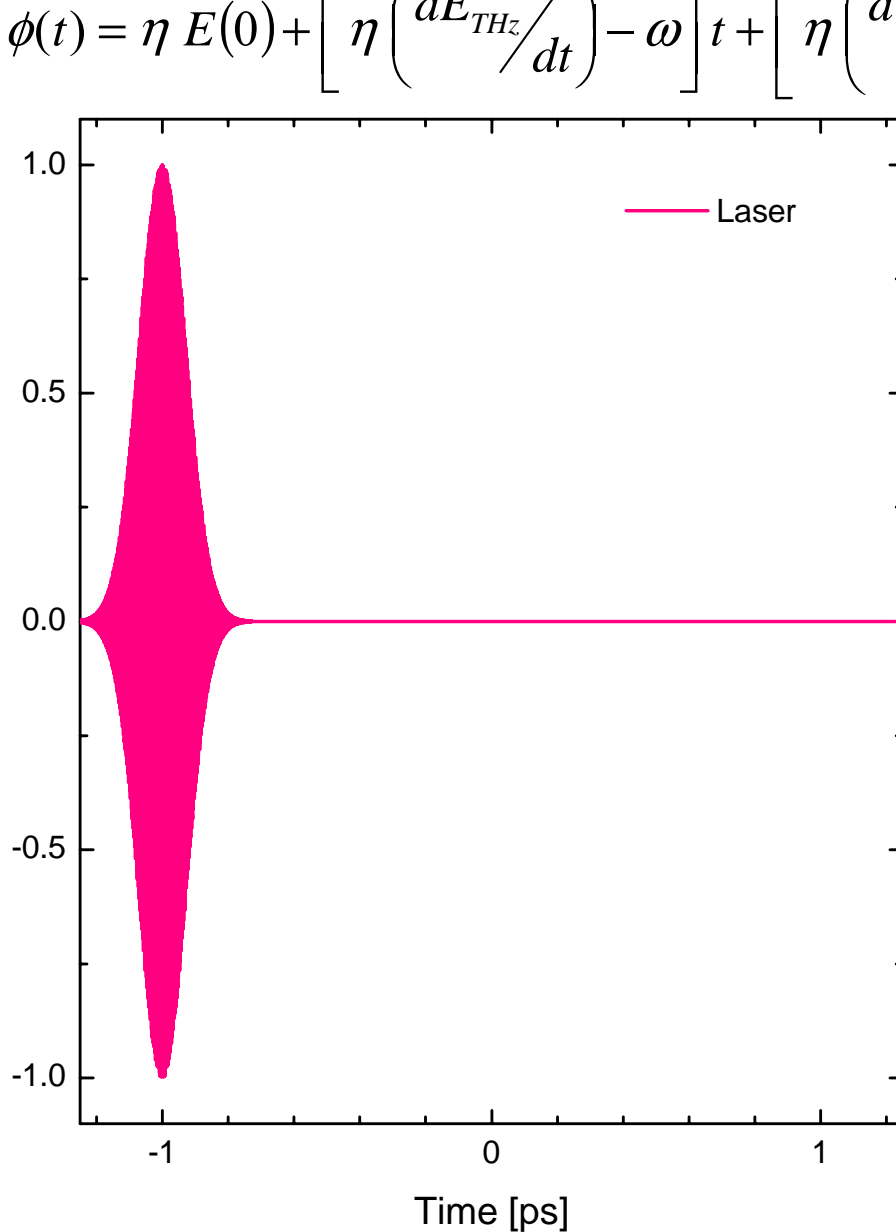


$$E(t) = E(t_0) + \frac{dE}{dt}(t - t_0) + \frac{1}{2} \frac{d^2E}{dt^2}(t - t_0)^2 + \dots$$



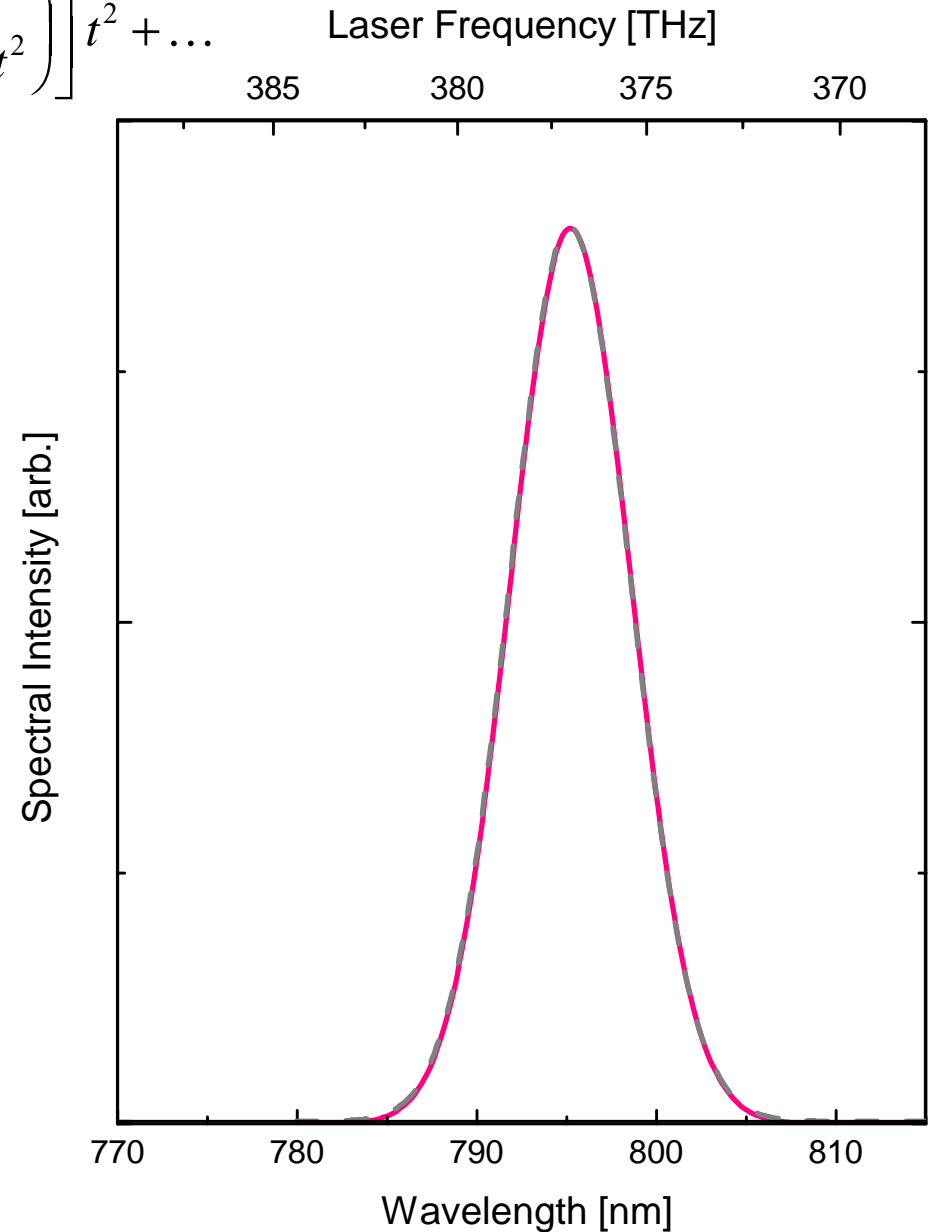
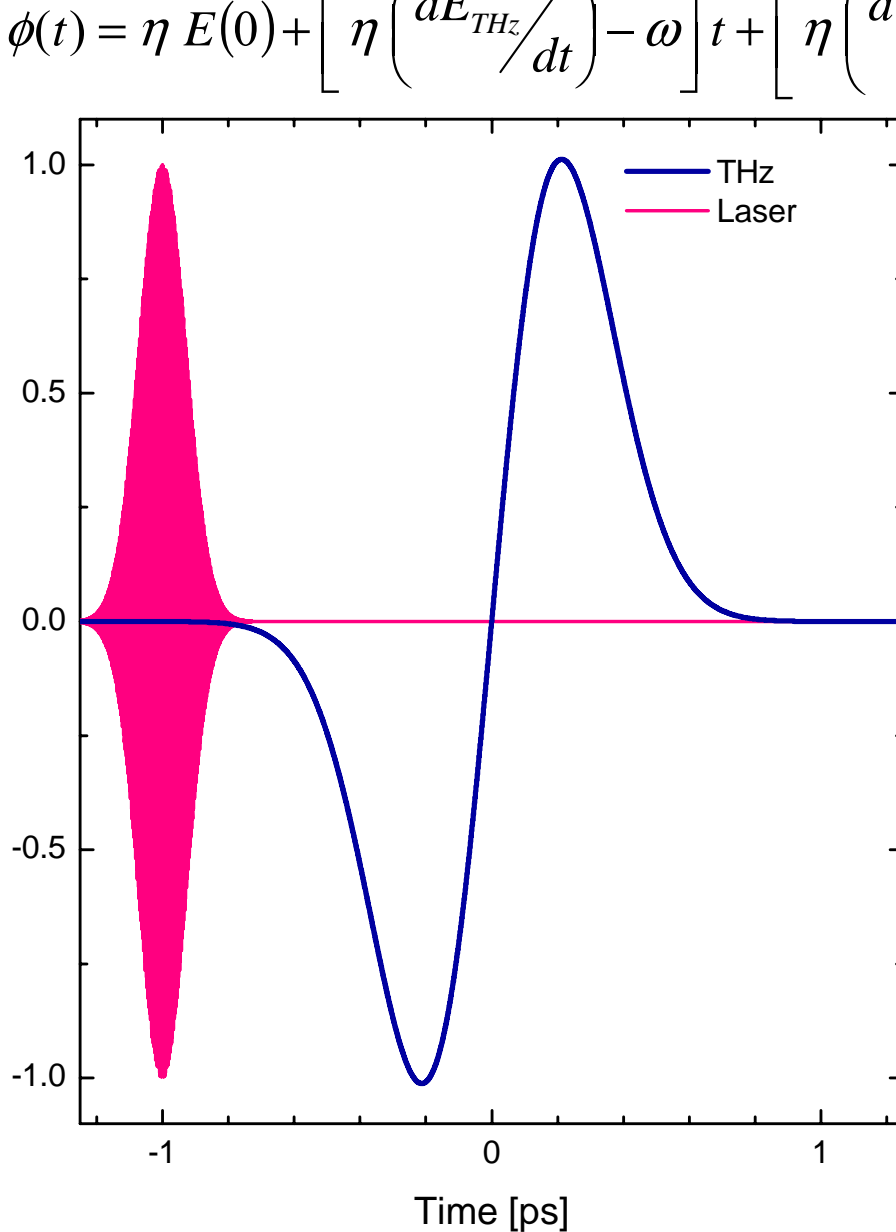
# Sampling Laser Pulse & Spectral Content

$$\phi(t) = \eta E(0) + \left[ \eta \left( \frac{dE_{\text{THz}}}{dt} \right) - \omega \right] t + \left[ \eta \left( \frac{d^2 E_{\text{THz}}}{dt^2} \right) \right] t^2 + \dots$$



# THz Phase Modulation of Sampling Laser

$$\phi(t) = \eta E(0) + \left[ \eta \left( \frac{dE_{\text{THz}}}{dt} \right) - \omega \right] t + \left[ \eta \left( \frac{d^2 E_{\text{THz}}}{dt^2} \right) \right] t^2 + \dots$$

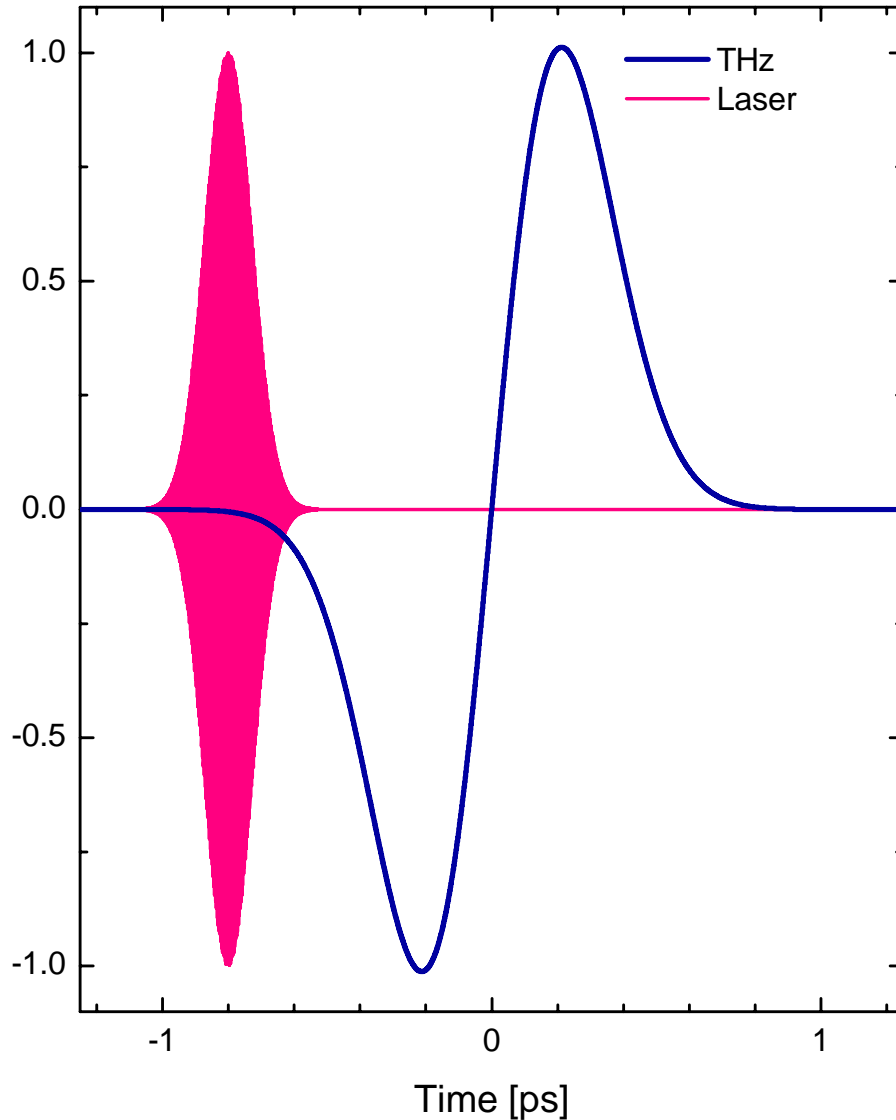


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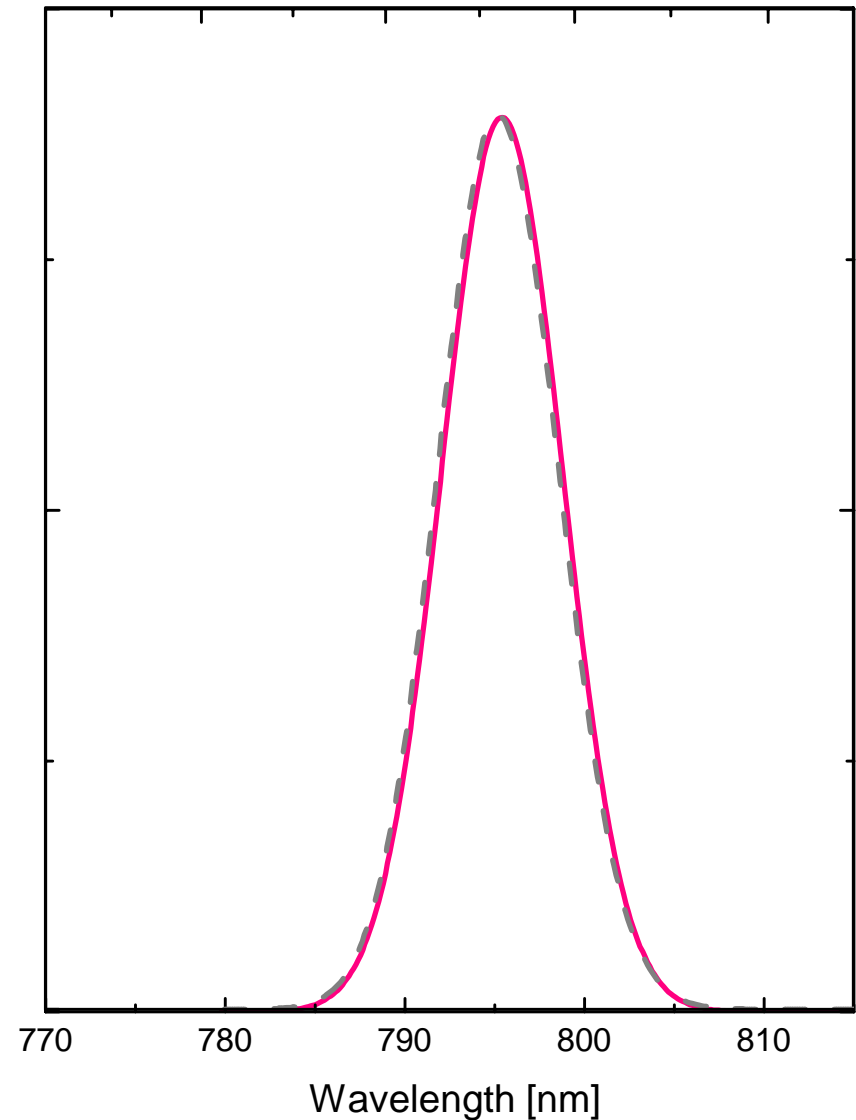
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Laser Frequency [THz]

385      380      375      370



Spectral Intensity [arb.]

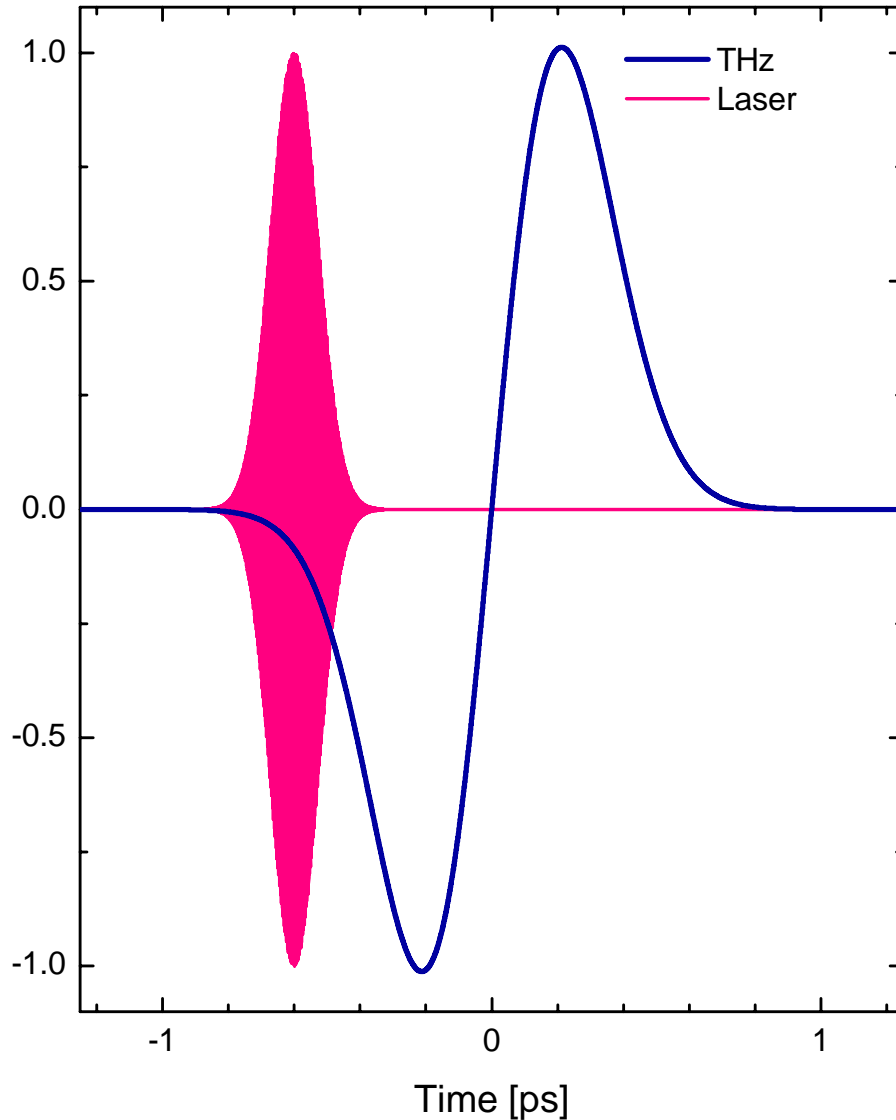


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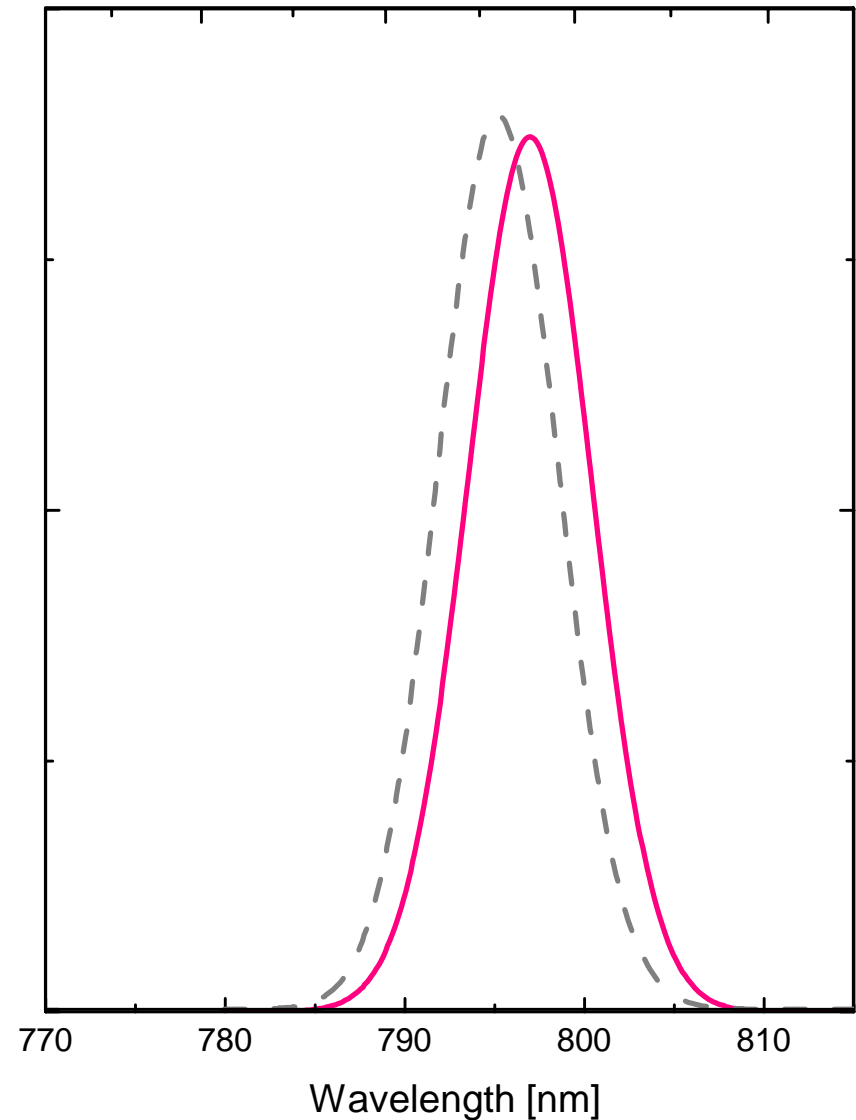
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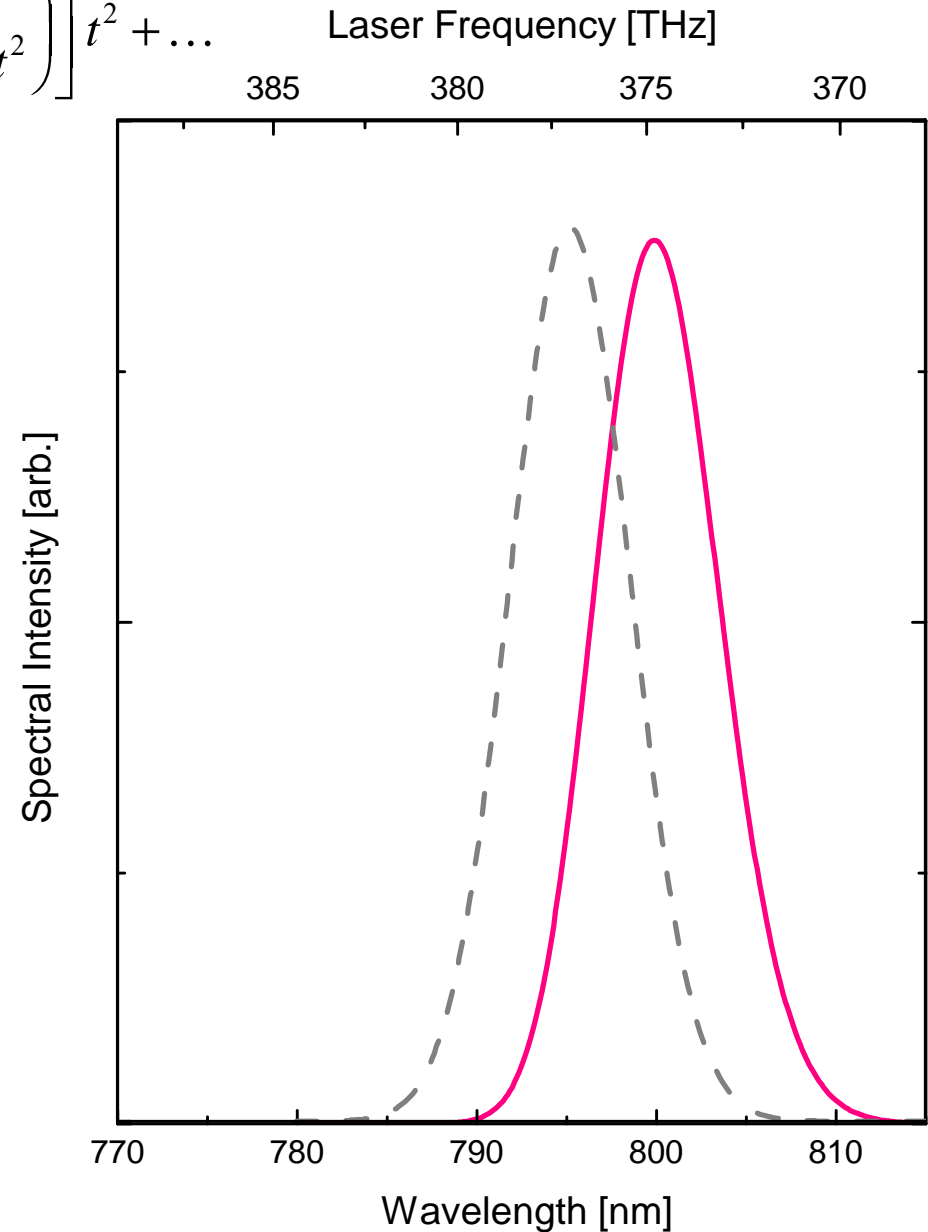
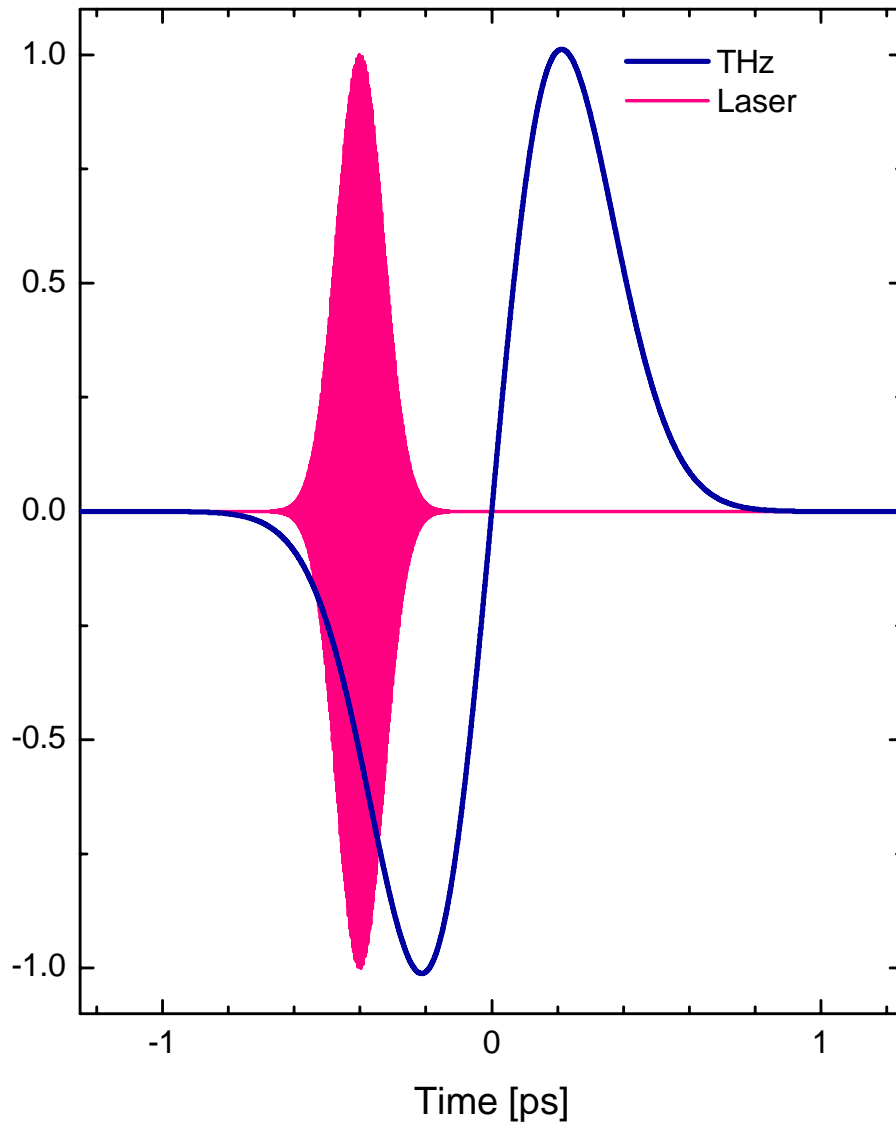


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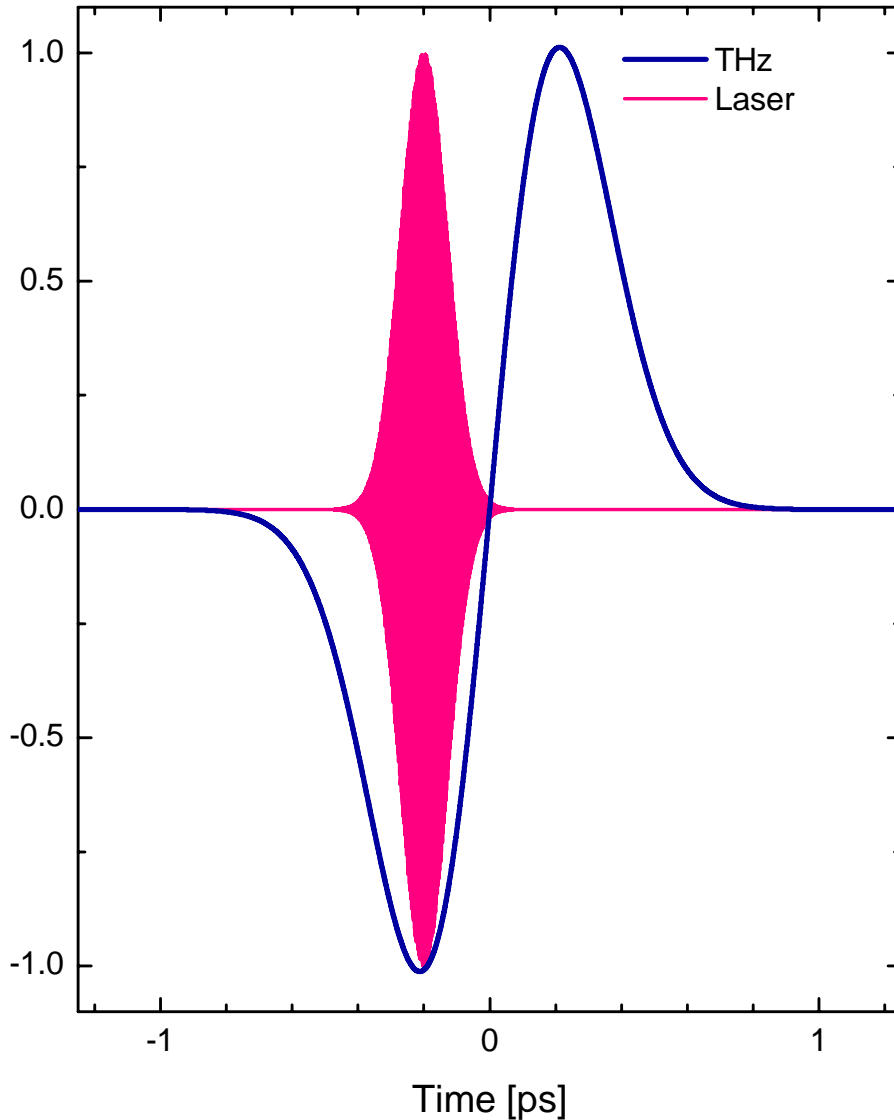


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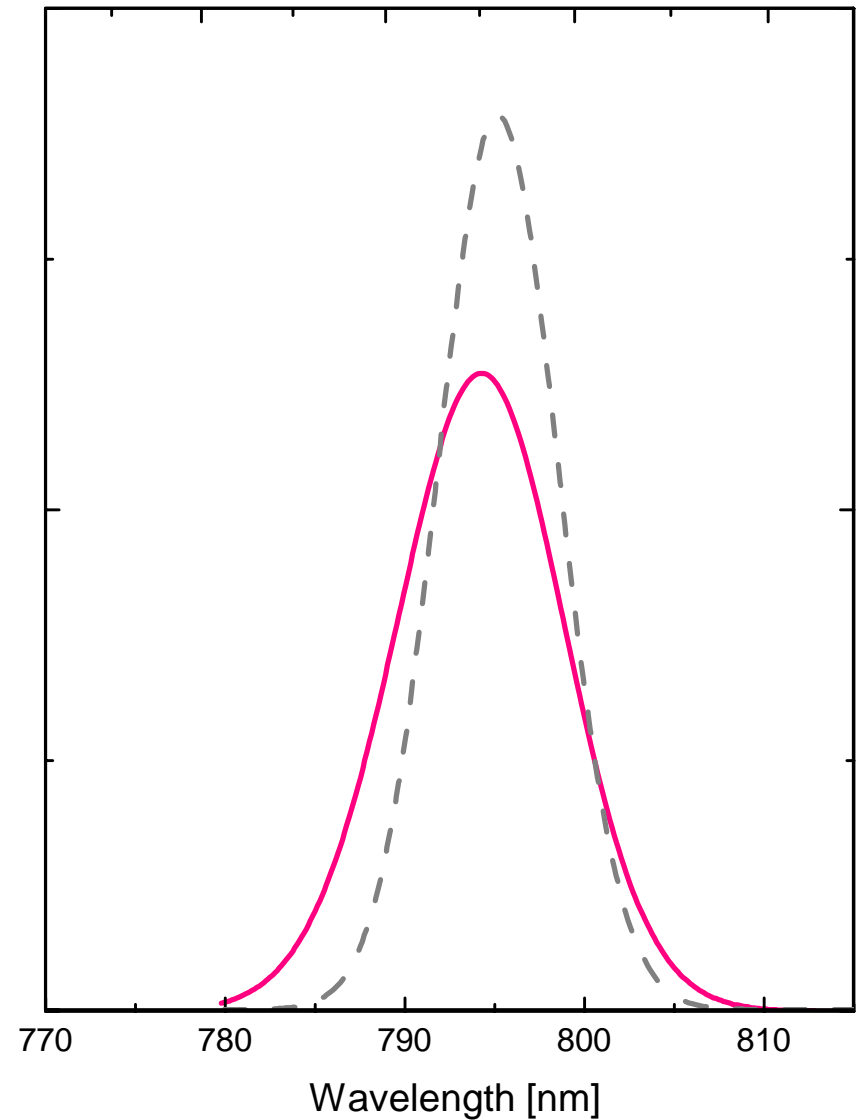
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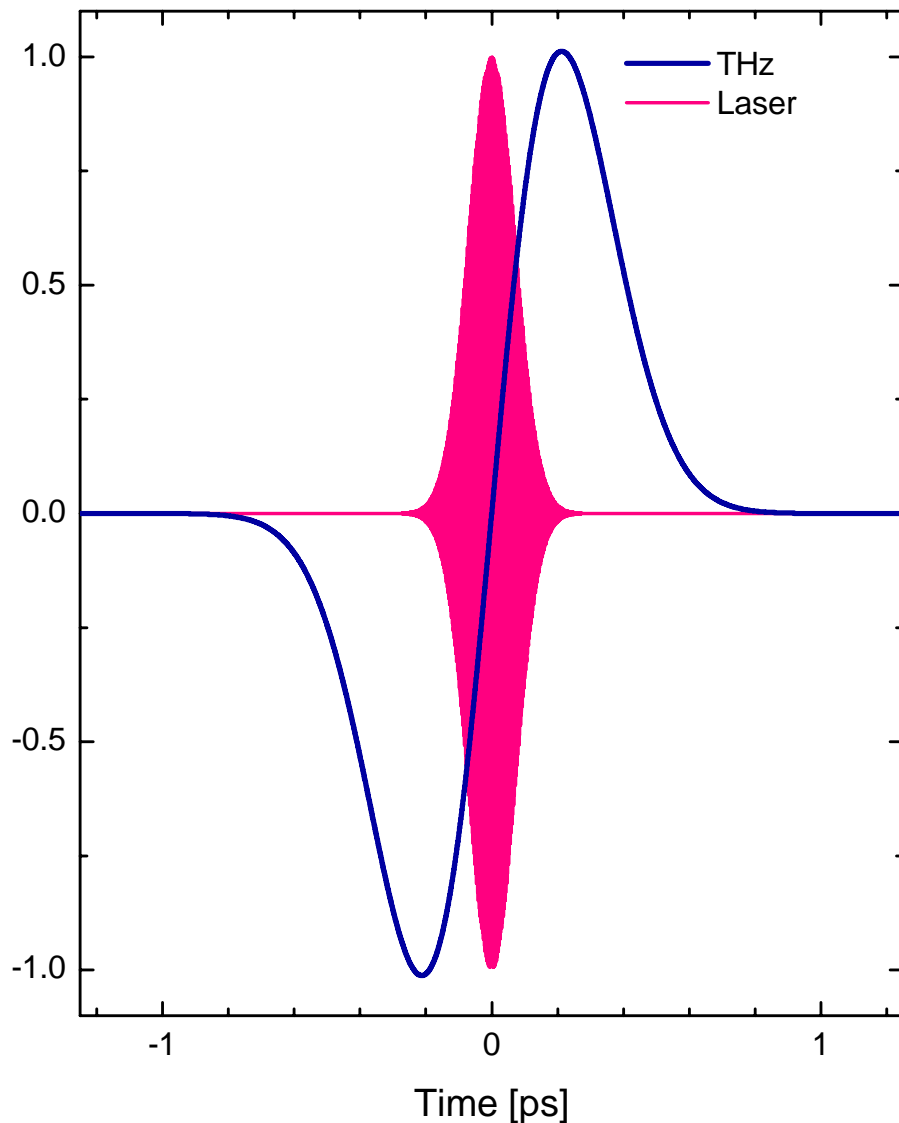


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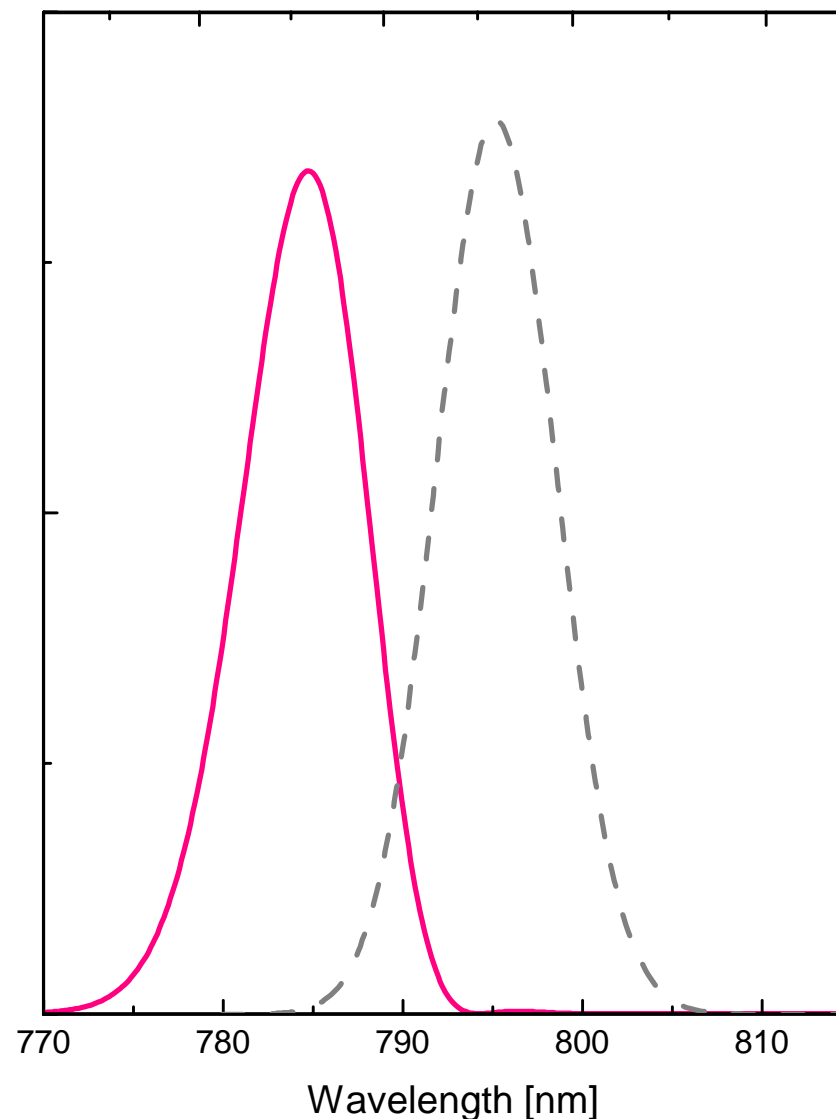
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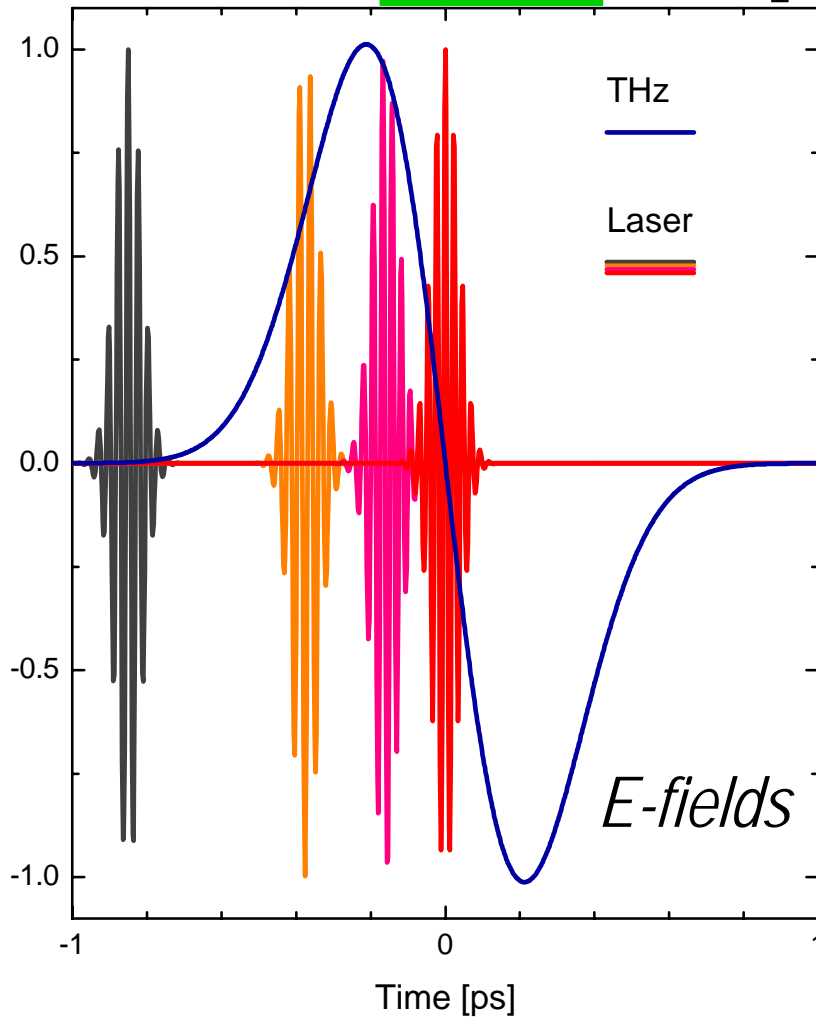


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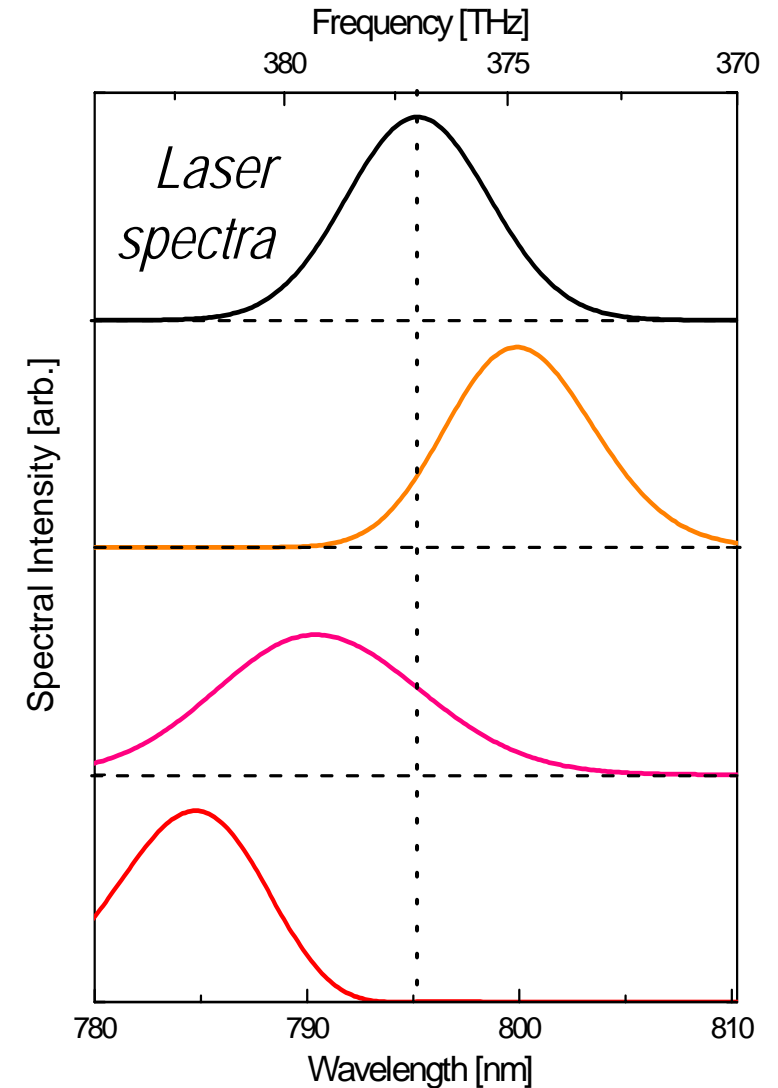


# Calculated Phase Modulation Effects

$$\phi(t) = \eta E(0) + \left[ \eta \left( \frac{dE_{THz}}{dt} \right) - \omega \right] t + \left[ \eta \left( \frac{d^2 E_{THz}}{dt^2} \right) \right] t^2 + \dots$$



500 kV/cm field  
0.5mm thick ZnTe

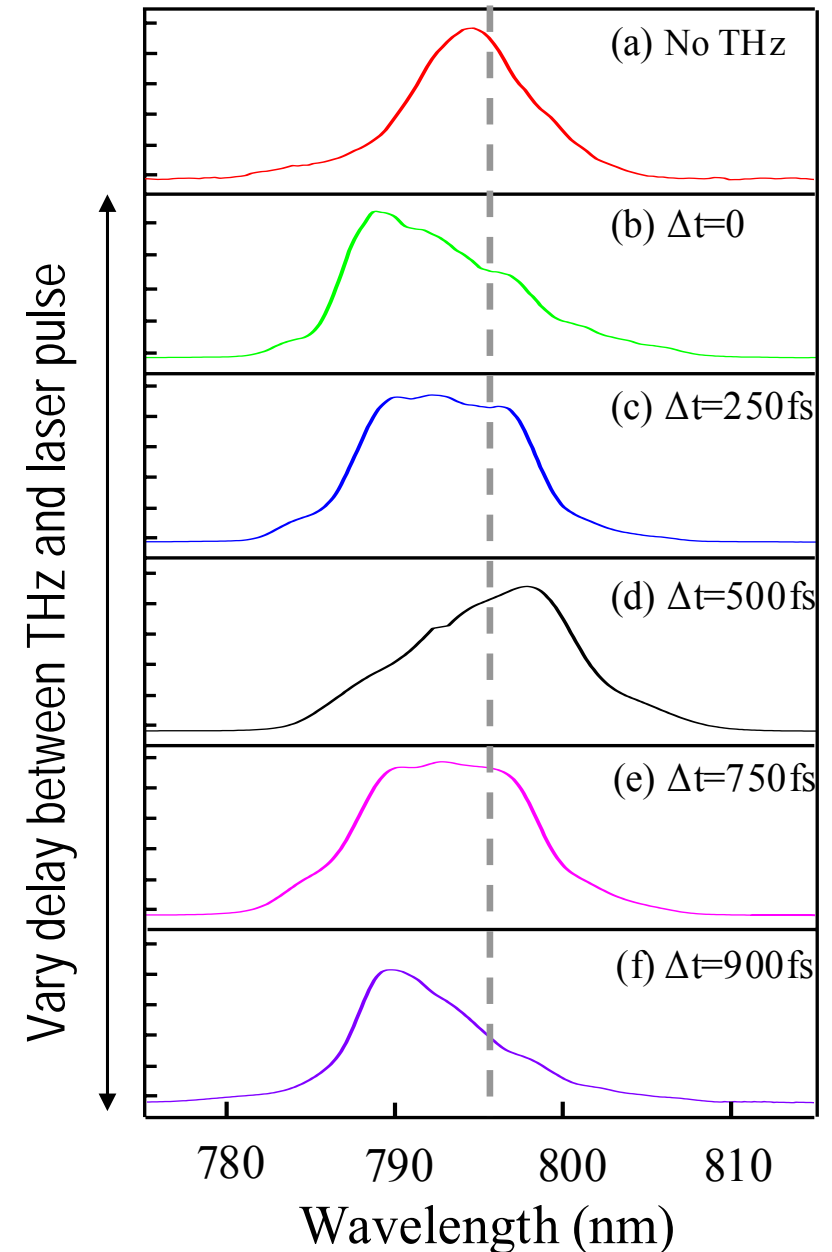


Other details: Lensing from spatial variation of  $n(t)$  (*time-dependent gradient index lens*)

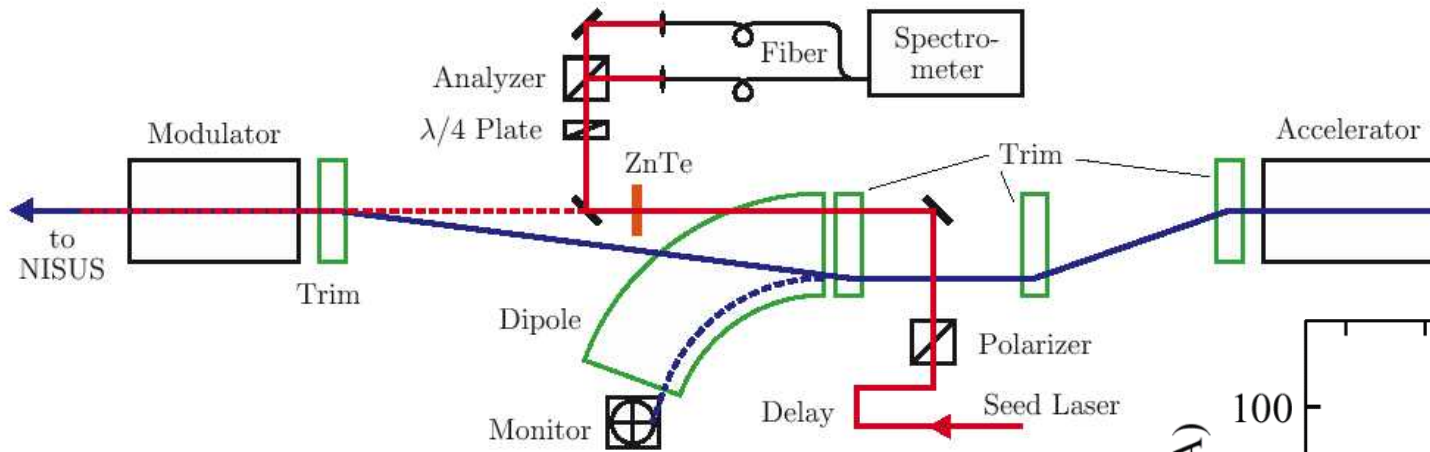


# Measured Phase Modulation with SDL Linac Coherent THz

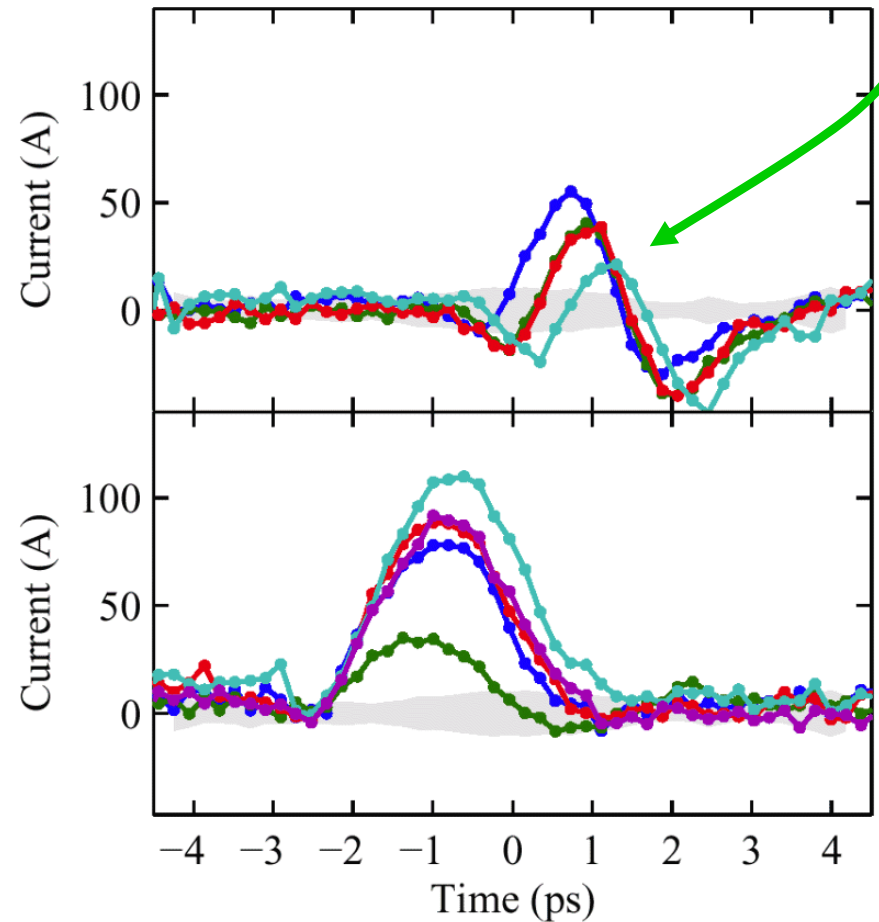
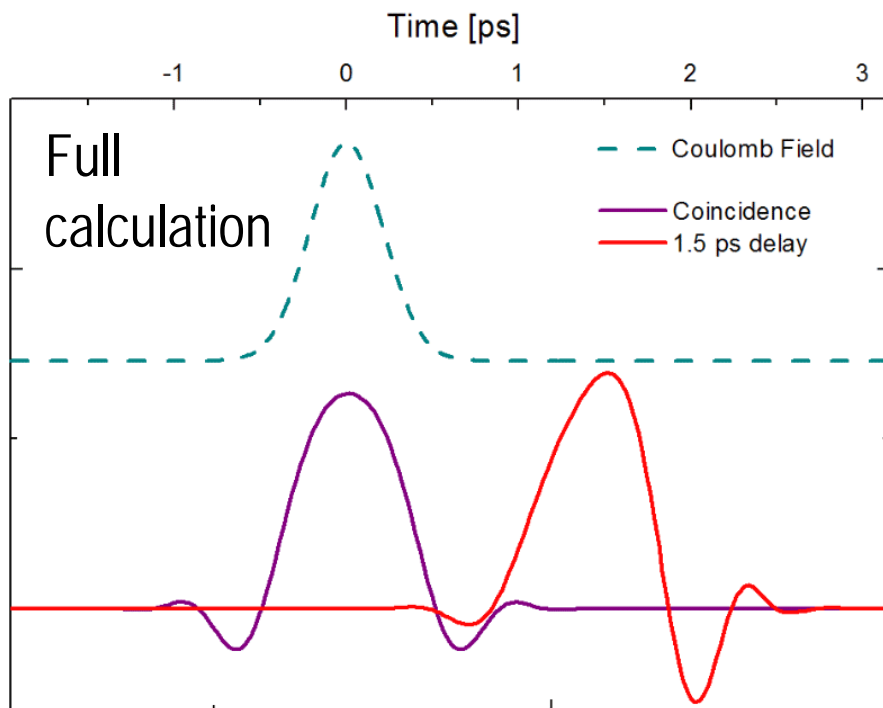
- Electro-optic measurements of SDL THz pulses.
  - 35  $\mu\text{J}$  pulses, 2mm focus, 0.5mm ZnTe.
- ~ 130 fs (FWHM) unchirped laser sampling pulse, no polarization analysis.
- Probably still a mixture of effects
  - optical alignment and waveform distortion
  - walk-off (velocity mis-match)
  - phase modulation (2<sup>nd</sup> and 3<sup>rd</sup> order NLO)
  - dynamic lensing that affects coupling into spectrometer's optical fiber.



# EO Detection of Bunch Coulomb Field (inside linac)

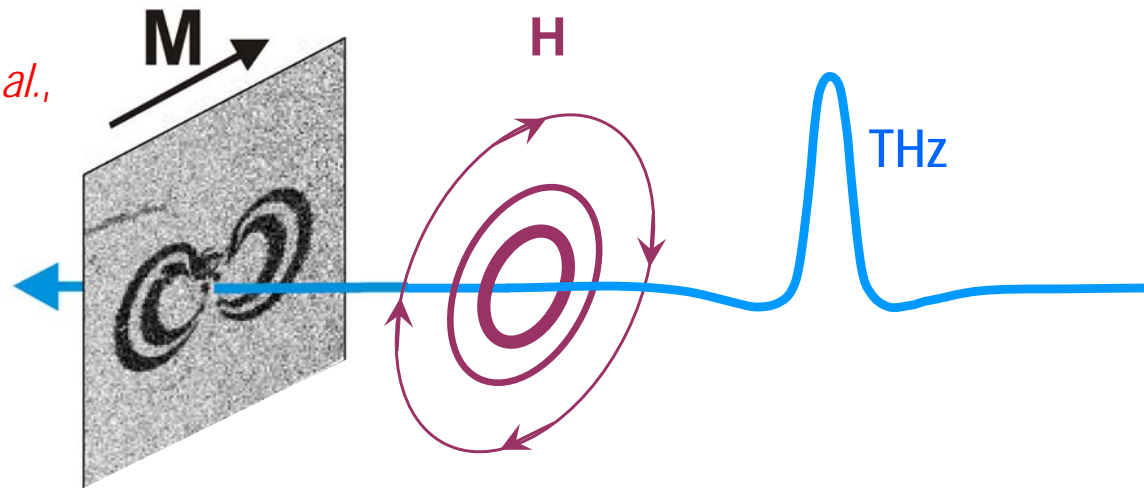


*X. Yan et al (PRL '00)*  
*I. Wilke et al (PRL '02)*  
*H. Loos et al (PAC '03)*



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Figure from C. H. Back, *et al.*,  
*Science* 285, 864 (1999)



- Idea:  
Use strong THz field to affect magnetization state of a thin film on  $< 10^{-12}$  s time scale.
- Ex situ approach  
Use propagating THz wave external to accelerator. Contrast study at SLAC/SPPS (Stöhr *et al*, *Nature*) where specimen was placed inside linac and directly exposed to electron beam.
- Method:  
pre-saturate film, expose to THz field pulse, then perform post image analysis (SEMPA)
- Similar approach could be used for the study of ferroelectric switching.

# Potential Application: Non-equilibrium Superconductivity

Superconducting state described by complex order parameter (amplitude and phase).

Most time-resolved studies have explored pair breaking and recombination (amplitude out of equilibrium) using  $\omega > \omega_g$  photons.

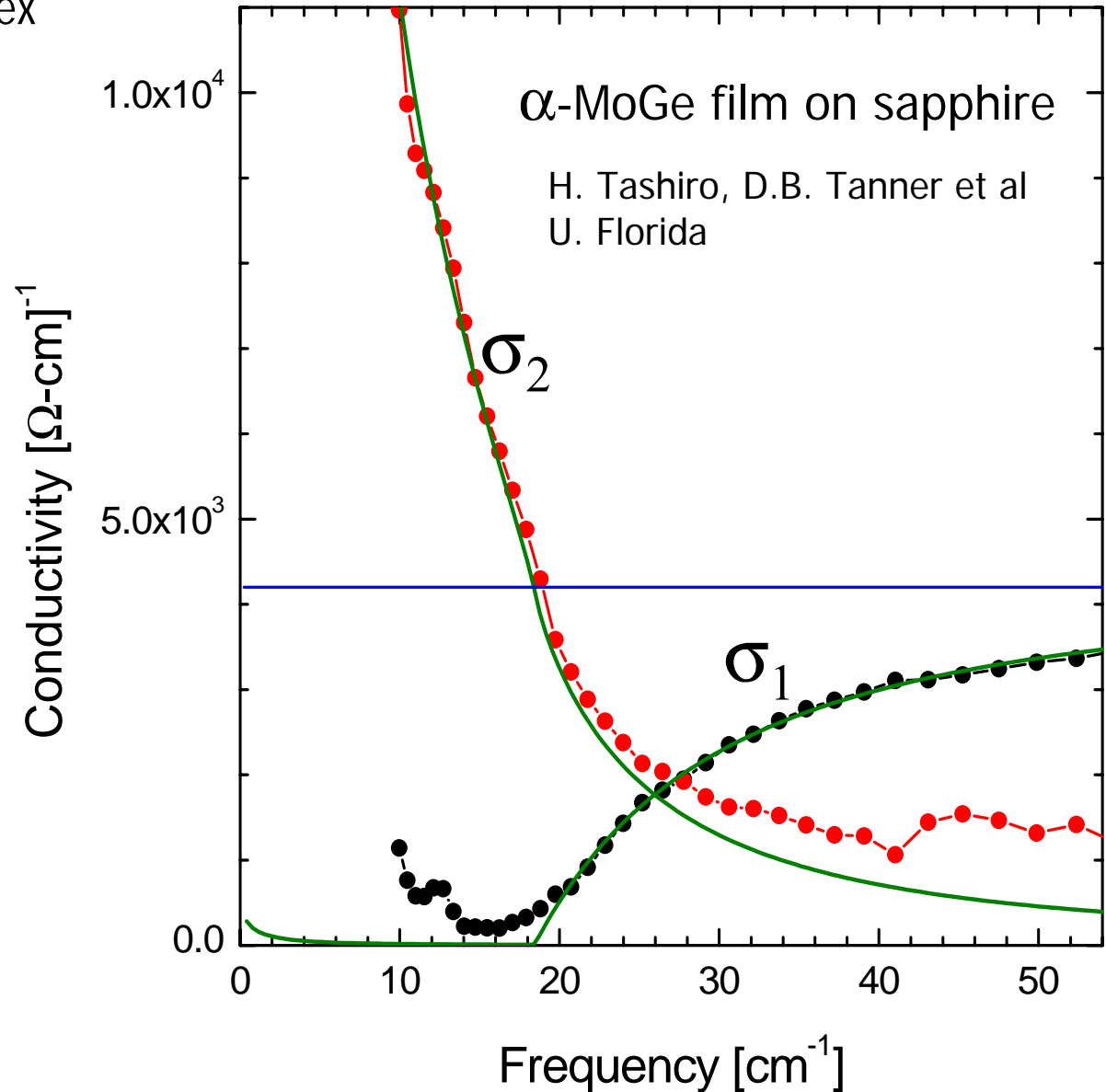
How does supercurrent (phase) react to a 1 MV/cm, ~ 1ps E-field transient?

Low frequency response is dominated by imaginary part of conductivity.

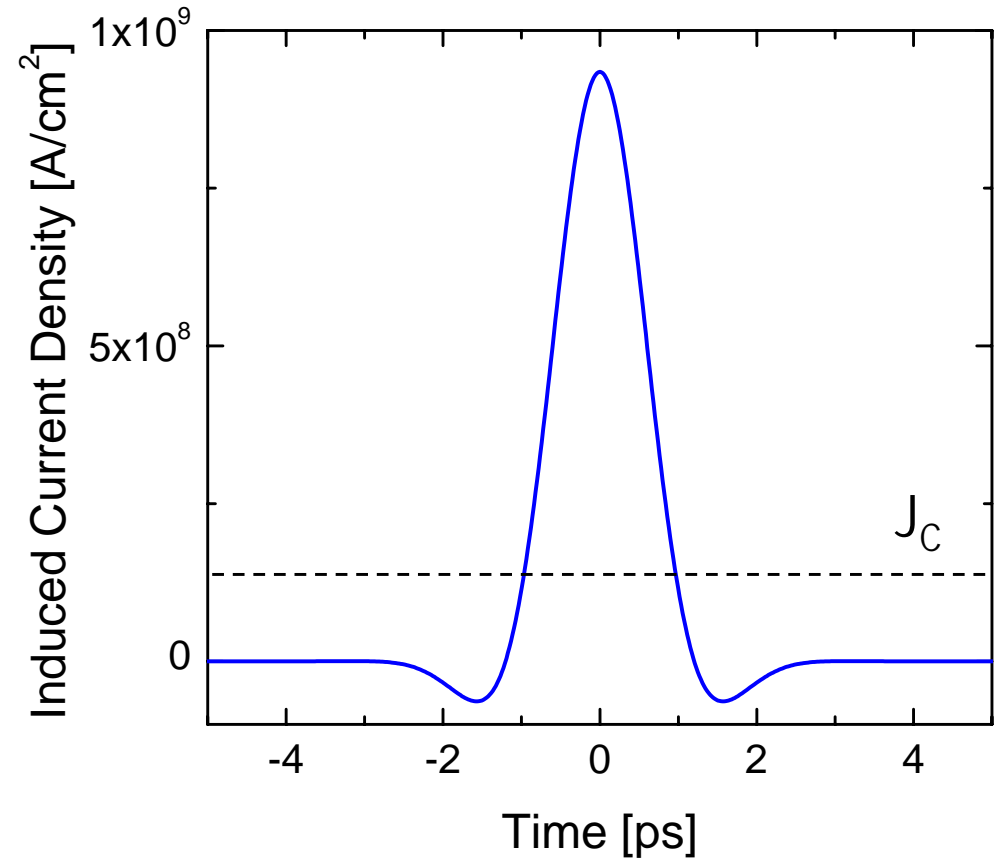
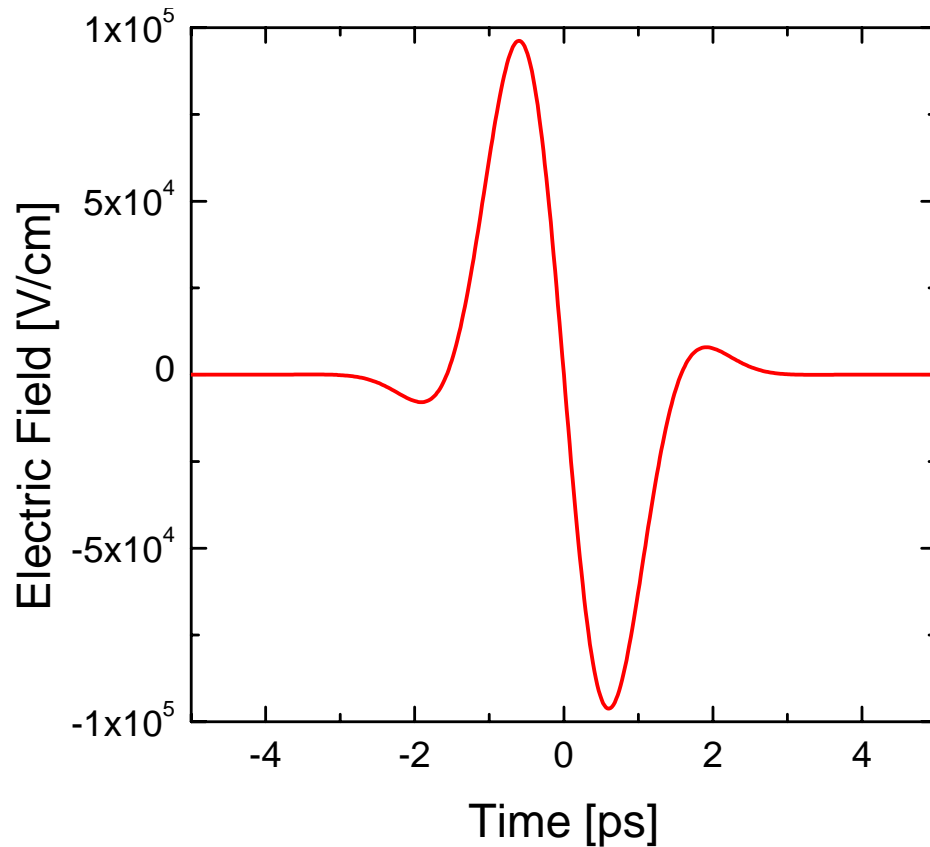
$$\sigma[\omega < \omega_g] \sim \frac{i}{\omega} \quad (\text{pure inductor})$$

$$L \frac{dI}{dt} = V \quad I(t) = \frac{1}{L} \int_{-\infty}^t V(t') dt'$$

$$J \cong \sigma_n \omega_g \int_{-\infty}^t E(t') dt'$$



# Time-dependent Supercurrent in a Thin Film Superconductor



Note: a typical superconductor has critical current  $J_C \sim 10^8$  A/cm<sup>2</sup>

=> "over twist" the local superconducting phase, spin off vortices?

How quickly can a vortex be created? How does dissipation initially appear?

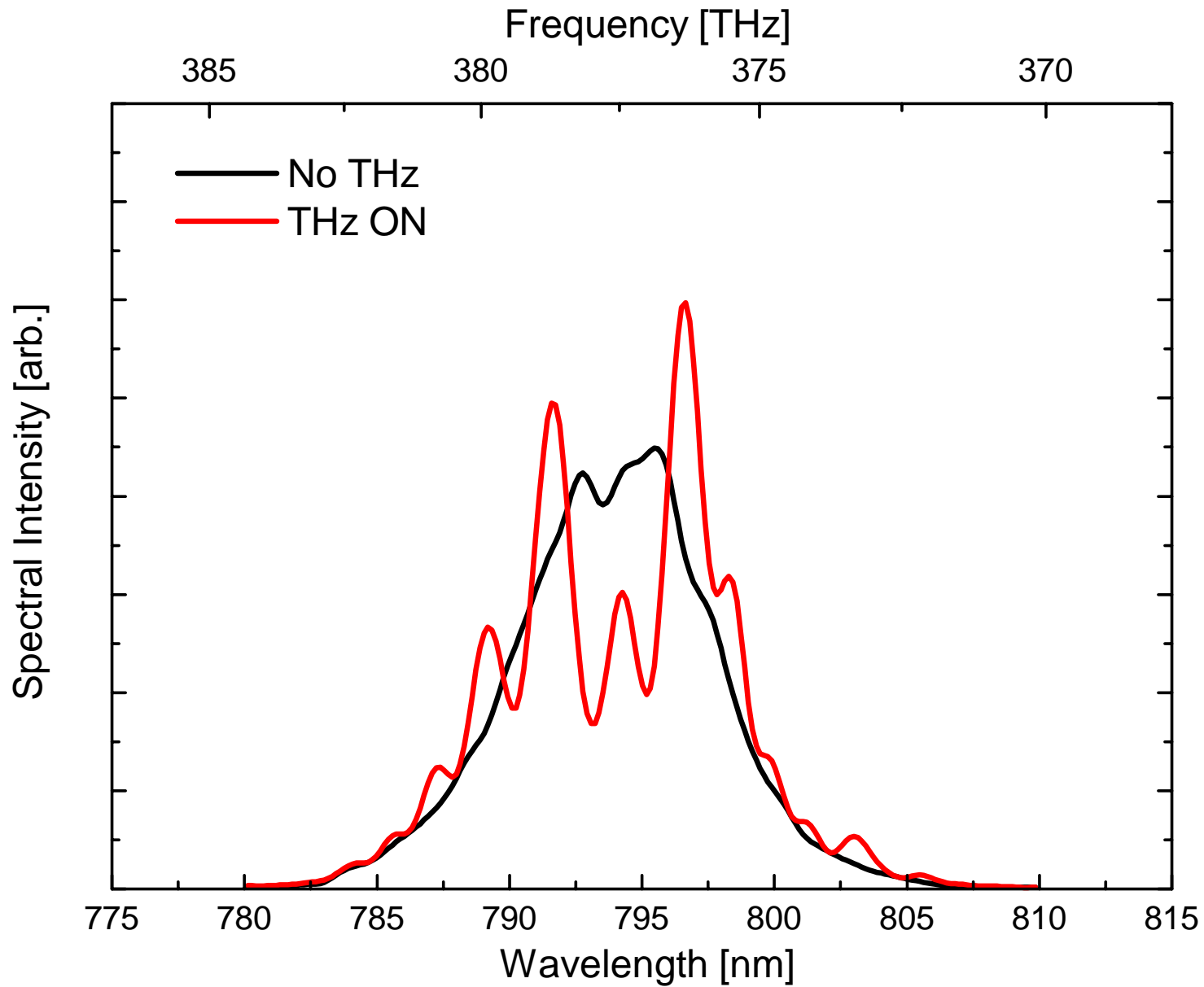
- Coherent SR bursts from NSLS VUV/IR ring
- Intense CTR pulses from photo-injected linac
  - single-cycle pulses
  - large electro-optic effects: time-dependence leads to laser phase modulation
    - spectral shifting & chirping
    - could be used to *control* ultrafast laser pulses.
    - affects in situ EO sampling of three-beam Coulomb field.
- Large pulse energy → strong electric (& magnetic) fields.
  - opportunity for studying field-induced ultra-fast switching.
  - initially: “photographic” samples
  - or waveform distortion in transmitted THz pulse.
  - ultimately: THz, other probe (x-rays, electrons)

*Acknowledgements: J. Misewich, G. Nintzel, R. Smith, B. Singh (Brookhaven),  
T.F. Heinz (Columbia), Dave Reitze (Florida)*

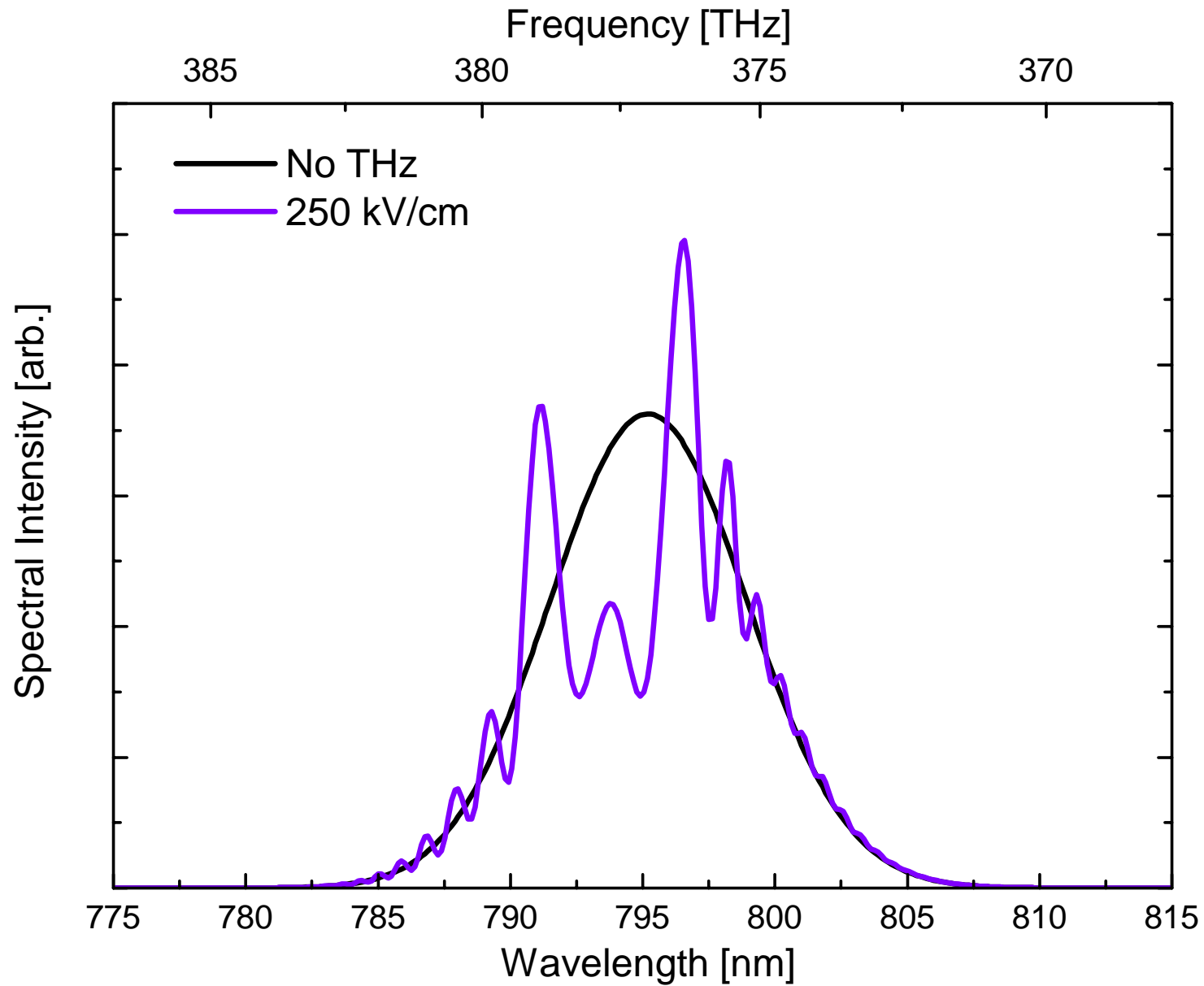
*end of slide show  
please applaud now*



# Single-Shot EO Sampling of SDL THz Pulse: Higher intensity

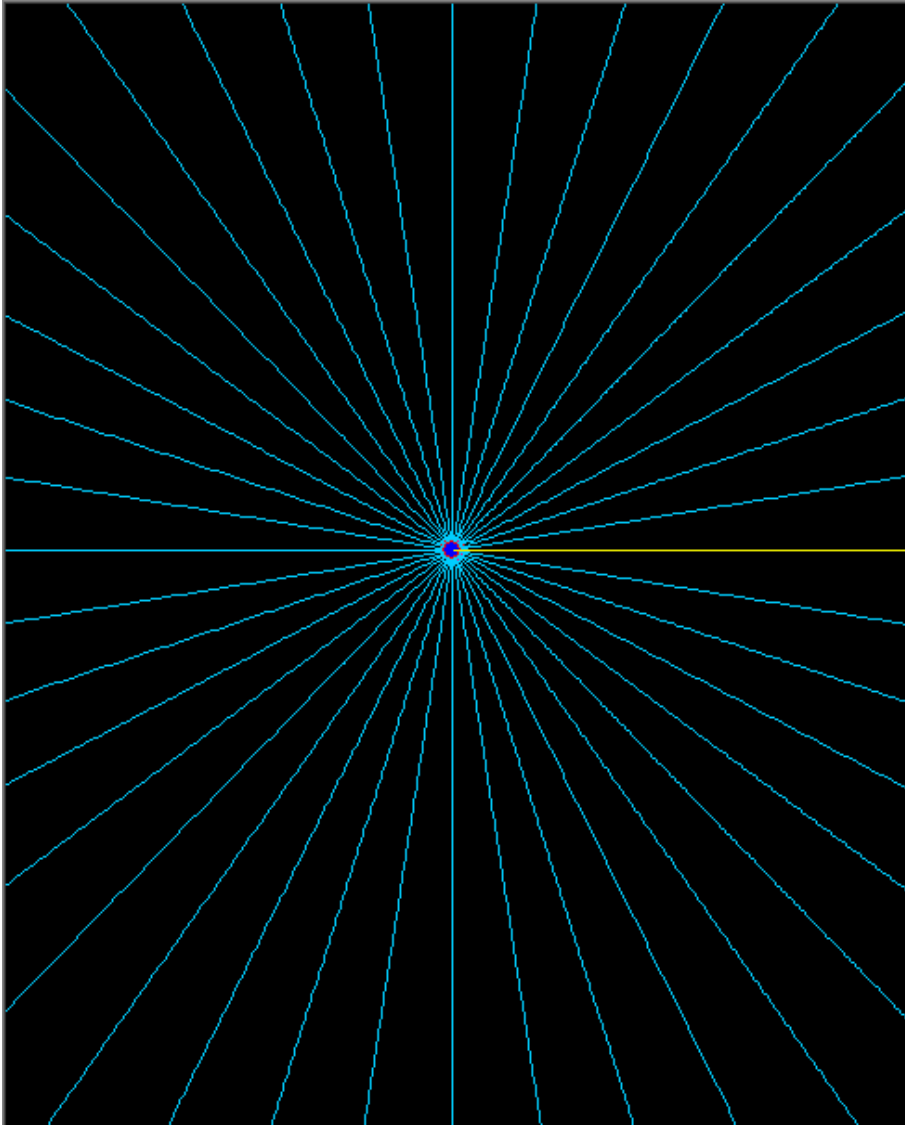


# Full Electro-Optic Calculation

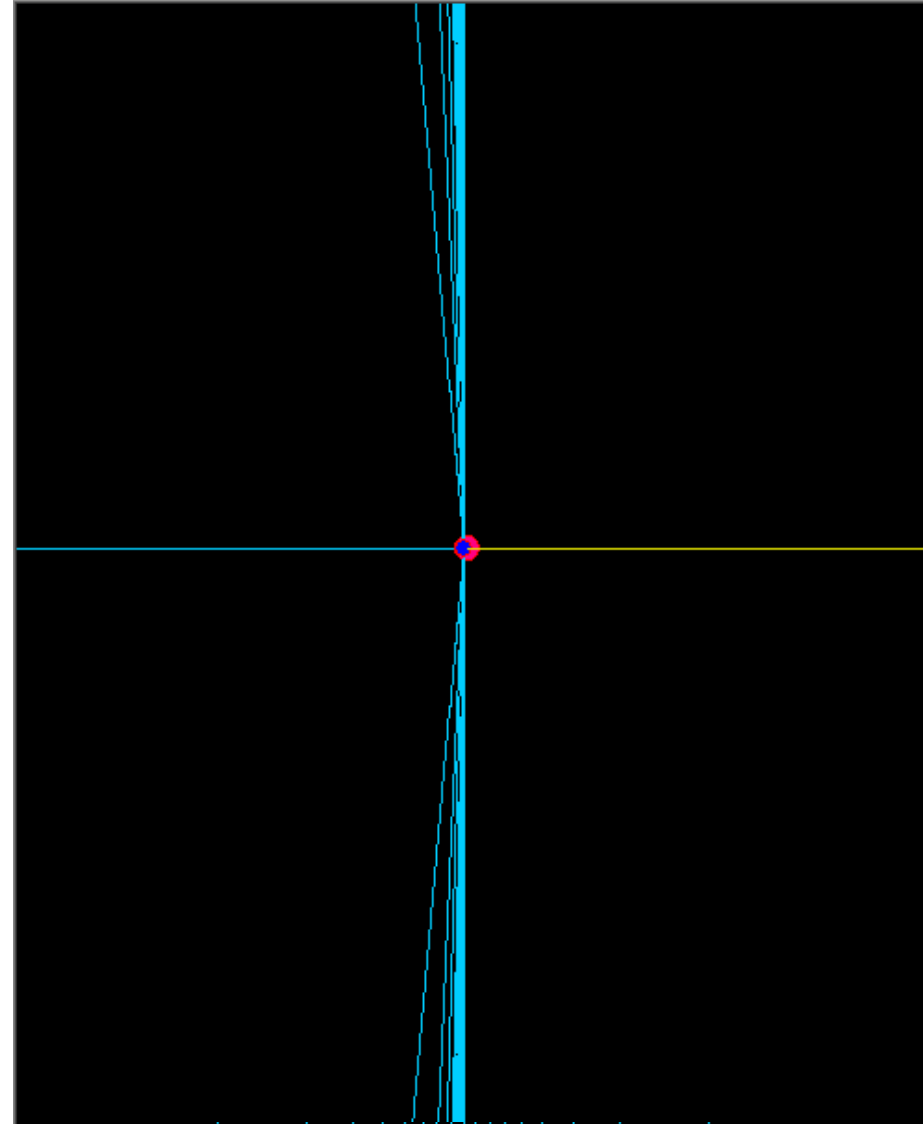


# Fields for Relativistic Electron

Non-relativistic Coulomb Field



Relativistic (1 GeV) Coulomb Field



# Radiation from Electron on Circular Orbit

Relativistic parameters

$$\beta = v/c \quad \gamma = \frac{1}{\sqrt{1-\beta^2}}$$

$$m = m_0\gamma$$

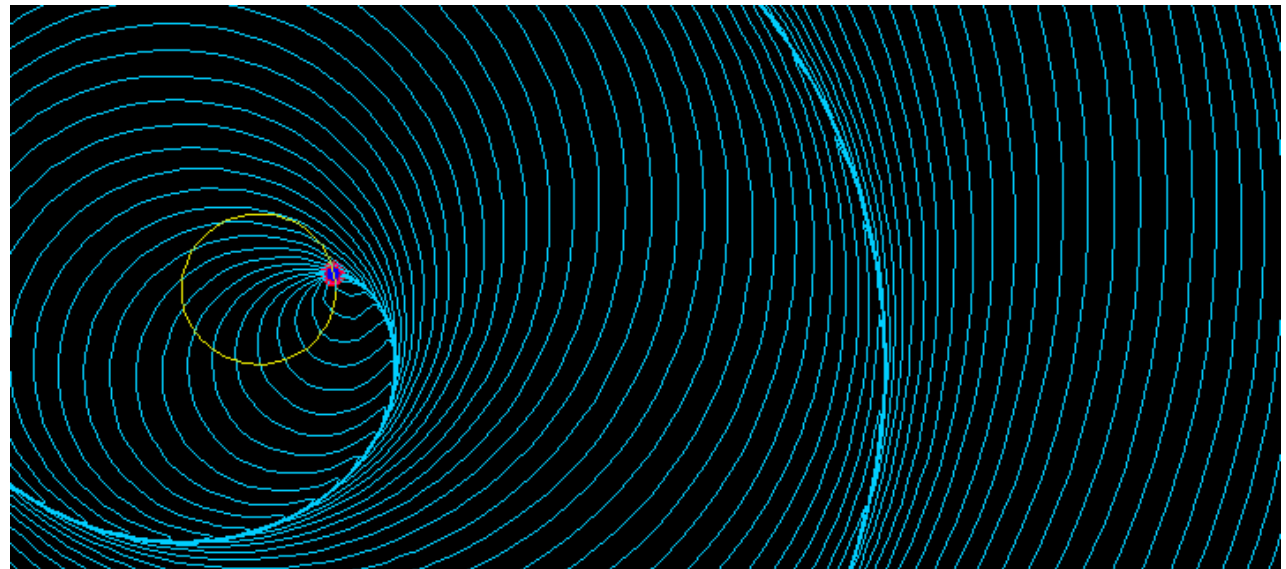
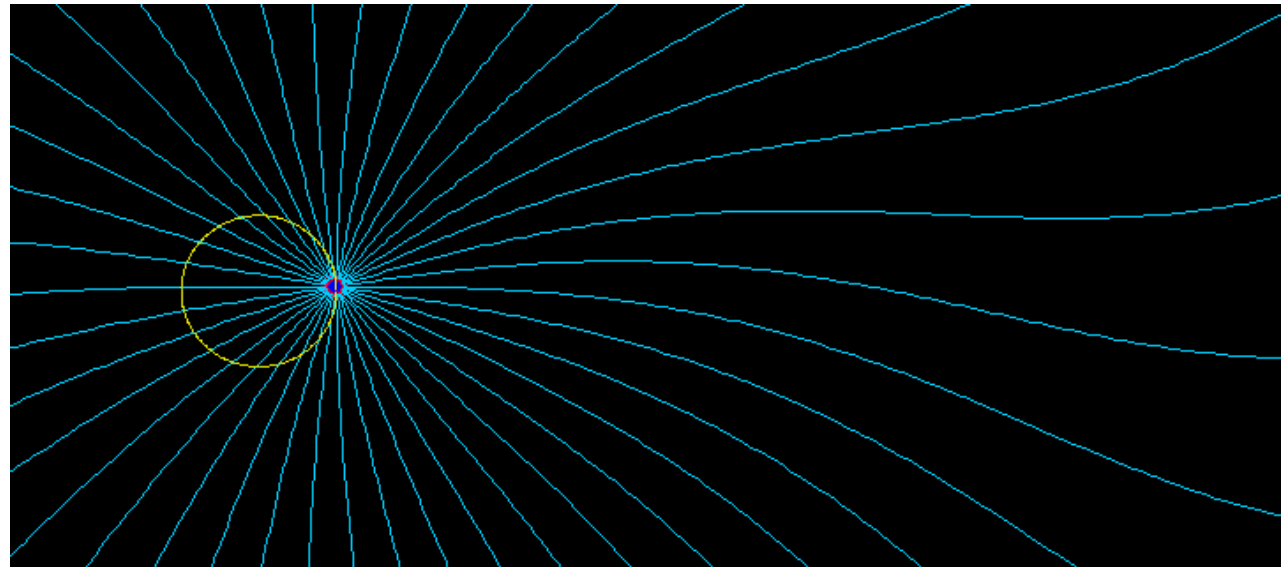
Modern accelerators:

$$\beta \sim 0.999999999$$

$$\gamma \sim 6000$$

$$\beta \sim 0.95$$

→

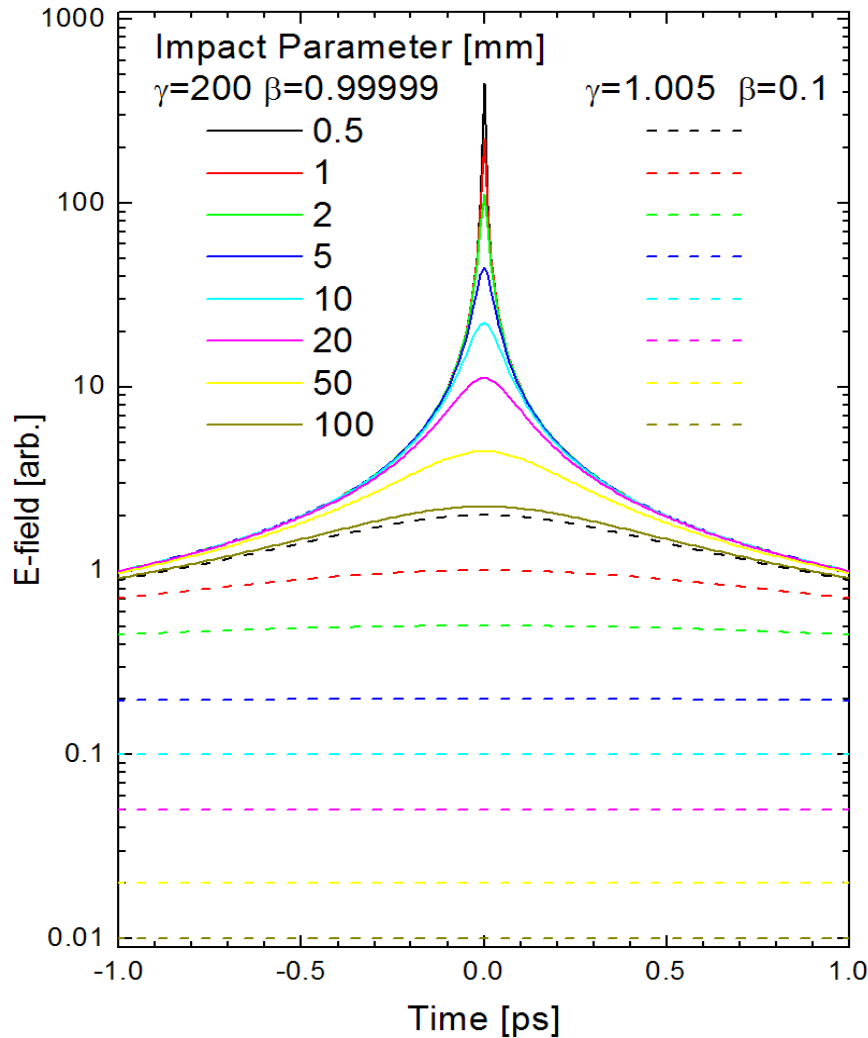


Calculated using  
Radiation2D code  
Tsumoru Shintake  
*RIKEN / Spring-8*

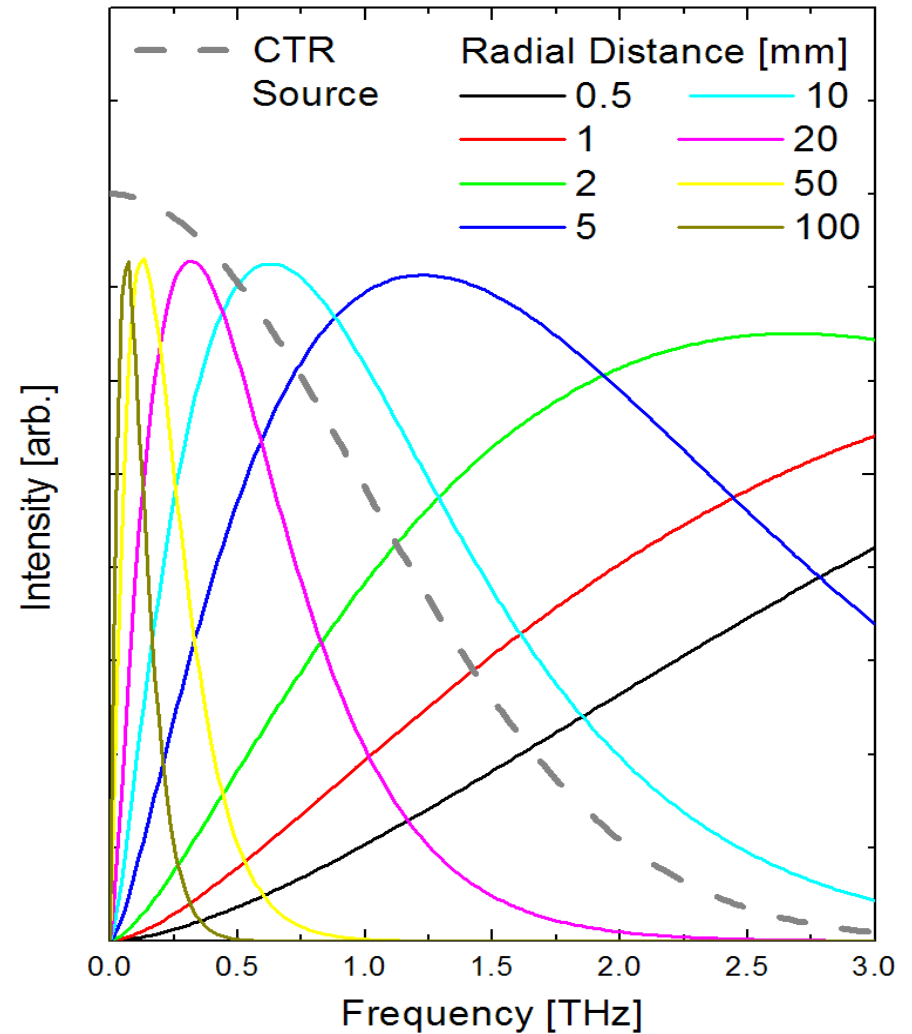
# Transition Radiation: Coulomb Field & Spectral Content

Radial Source Size ("waist"):  $W \sim \lambda\gamma/2\pi$

Time-dependent Coulomb field



Spectral Content (not to scale)

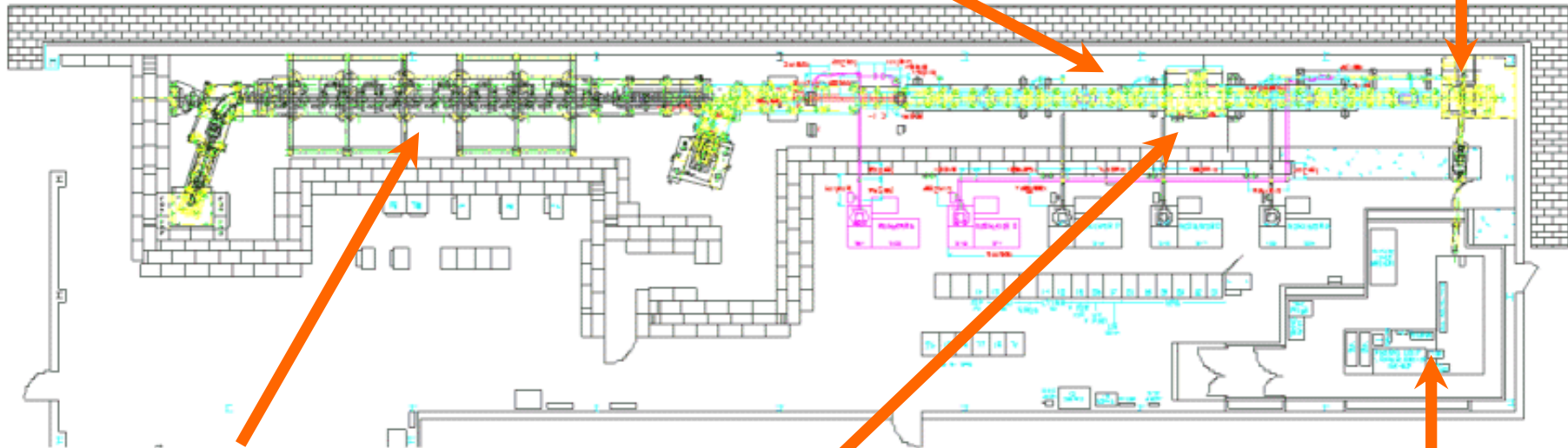
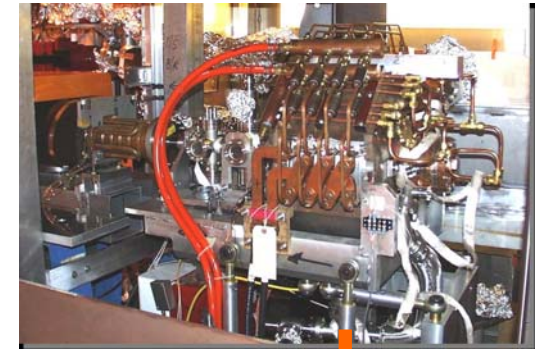


# Short Bunch Source: The NSLS Source Development Lab Photo-injected Linac

**300 MeV  
S-Band Linac  
(DARPA)**



**BNL  
Photo-injector IV**



**10 m NISUS Wiggler (SDI)**



**Chicane Bunch Compressor**



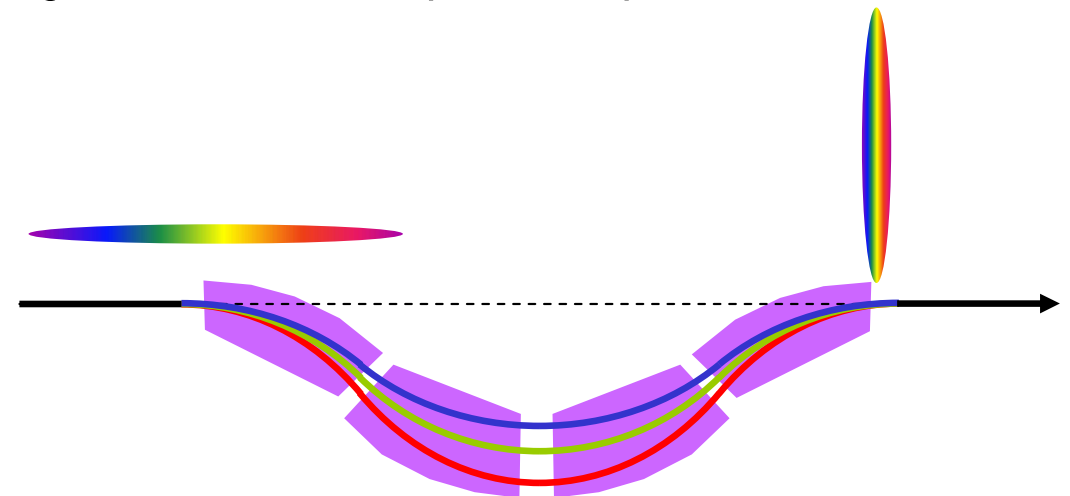
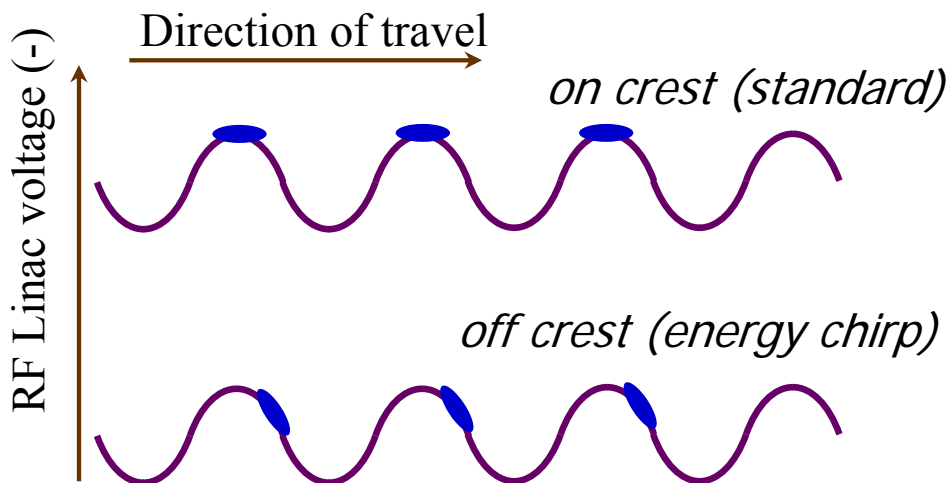
**Ti:Sapphire Laser**



# Making Short Bunches

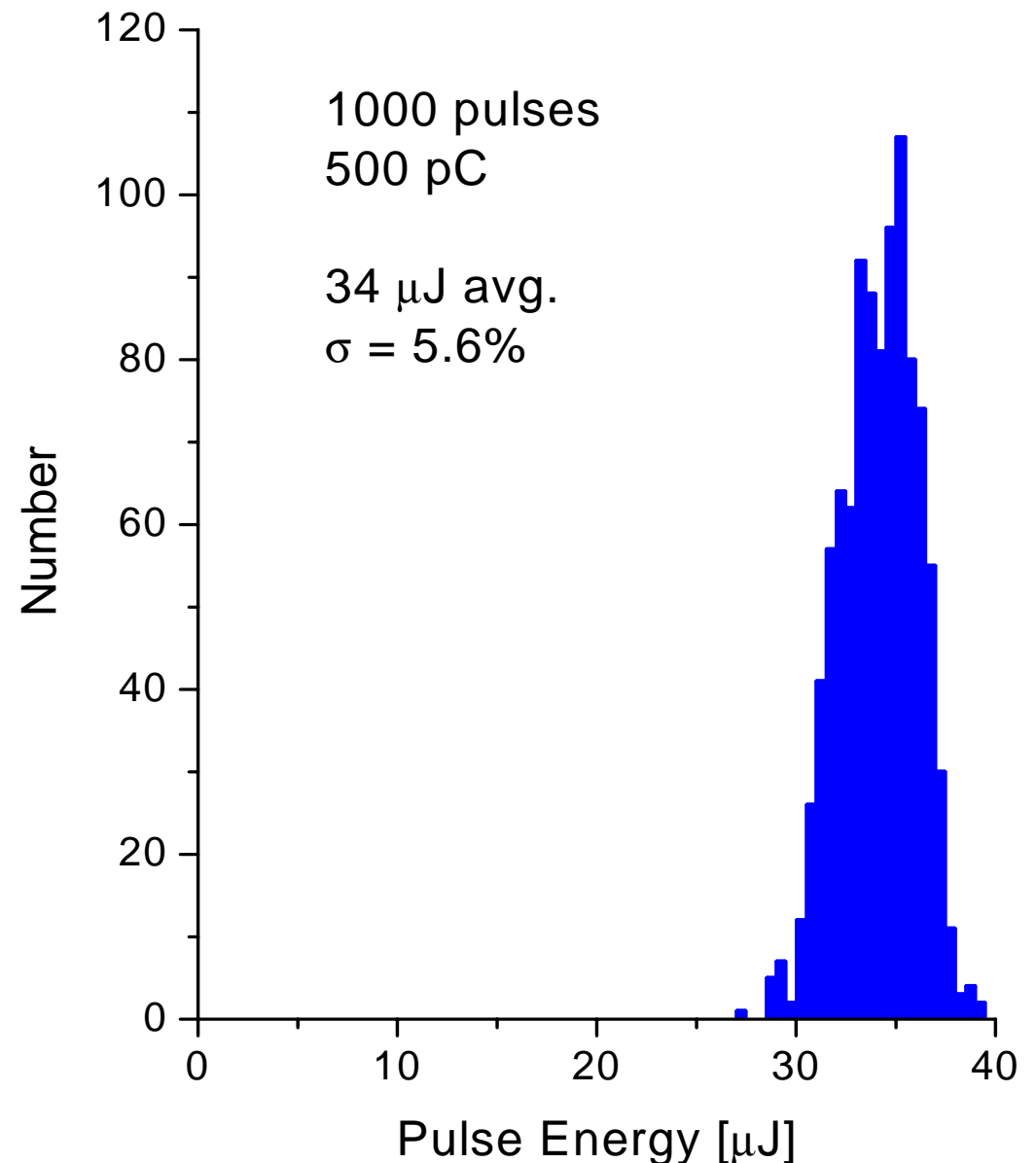
- Problem: Electron charge → Coulomb repulsion
  - Coulomb interaction causes spread in the energy distribution of a bunch.
  - For a non-relativistic electron, energy spread => velocity spread => distance spread.
  - BUT: For highly relativistic electrons, velocity spread remains small (*mass varies*).  
=> Start with long bunch, accelerate to high energy, then compress.

Compression method analogous to light, magnets serve as dispersive optics for electrons.



Dipole chicane to compress chirped bunch

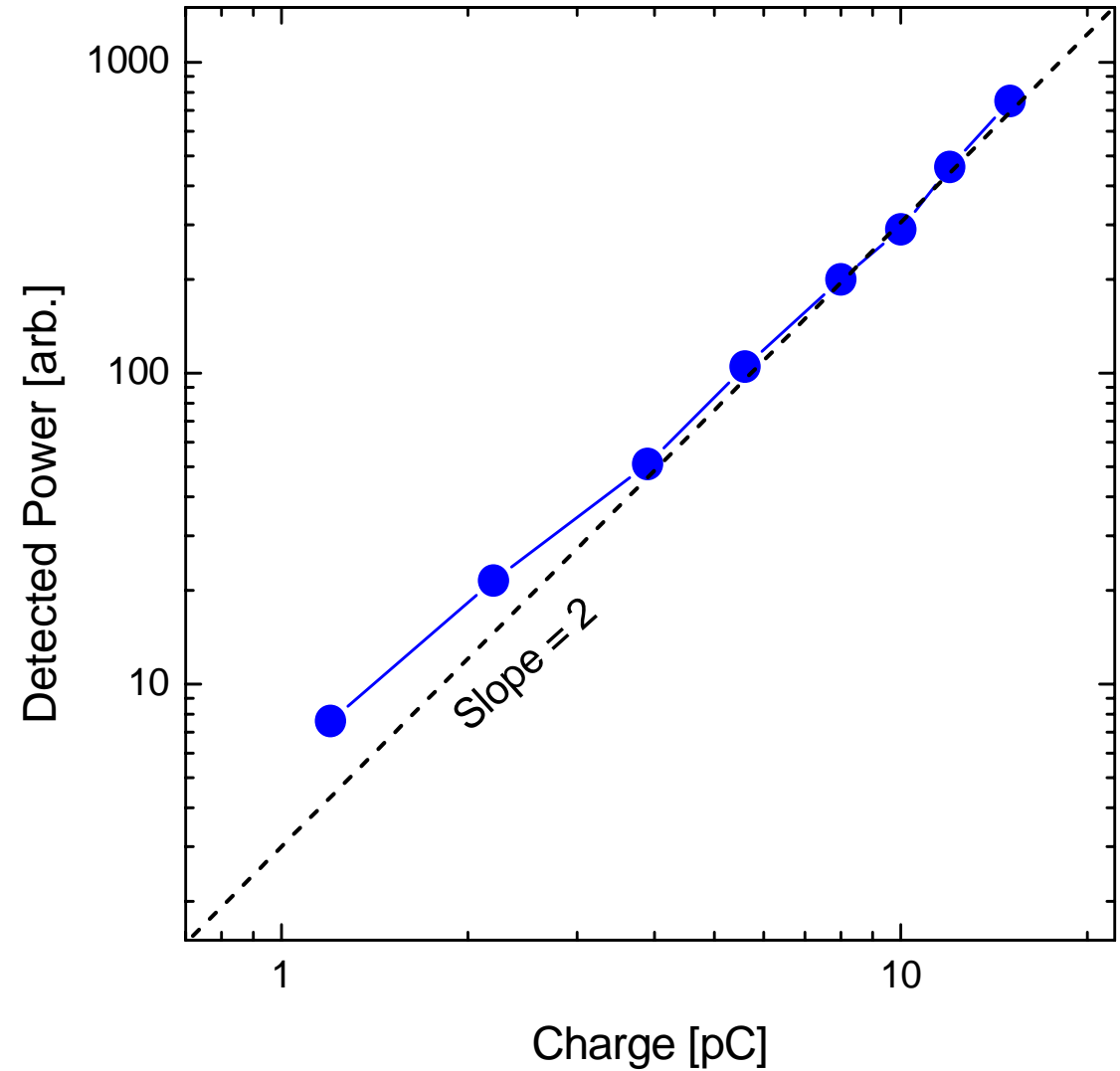
- Shot-to-shot fluctuations affect usefulness of pulses for some applications.
  - Interferometry
  - Pump-probe spectroscopy
- Typical fluctuations 4 to 6% RMS.
  - due mostly to variations in charge (particle number) from laser fluctuations.
- High rep. rate (average) or single-shot capability needed.





# $N^2$ dependence

- Intensity  $\sim Q^2$  ( $\propto N^2$ ) is a signature of coherent emission.



# Opportunities in Magnetism with THz Pulses

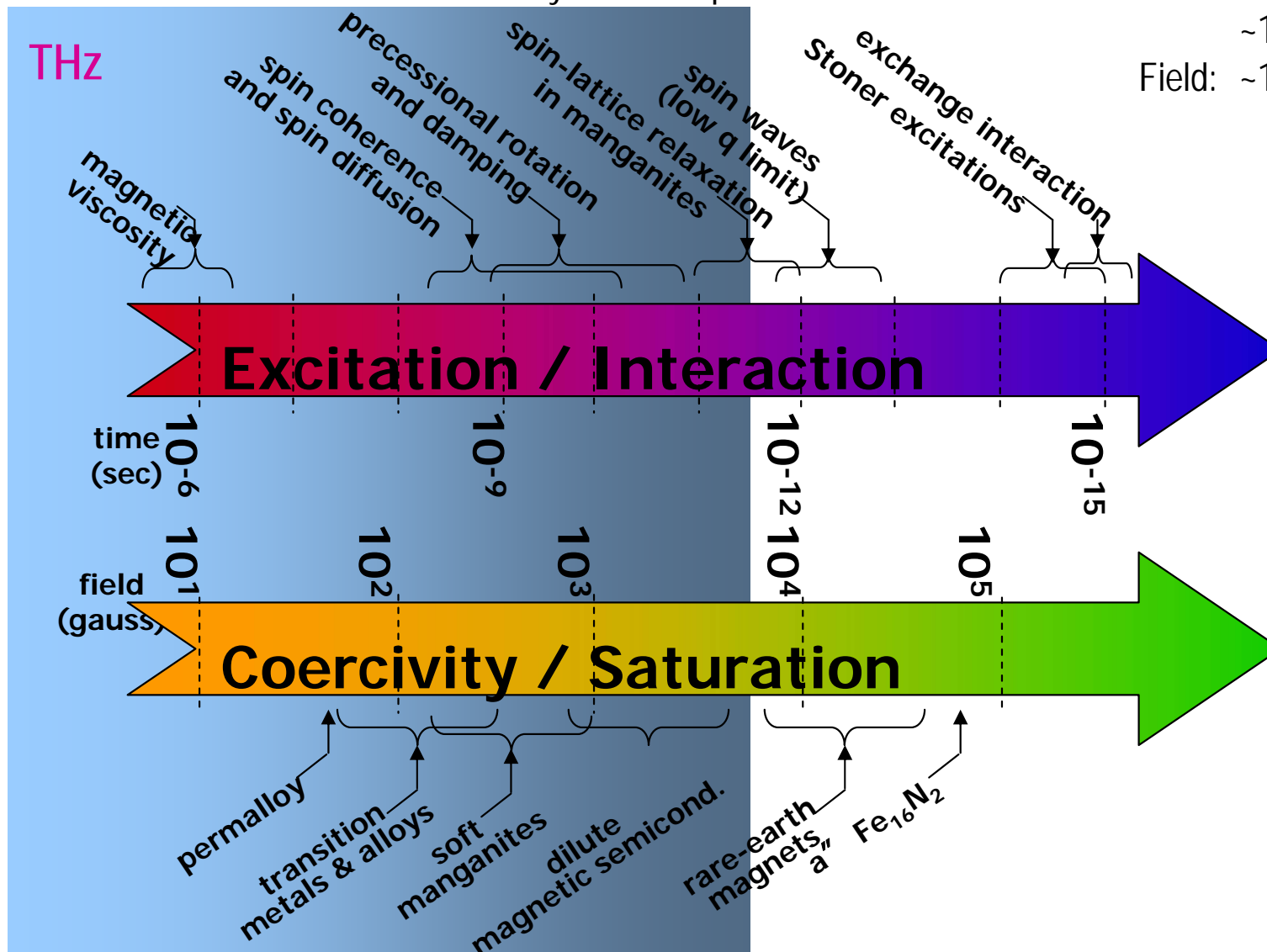
## Ultra-Short Pulses and/or High Fields -- D. Arena / NSLS

Current state of the art for "ultra-fast" dynamics experiments:

Time: ~100 fs (lasers)

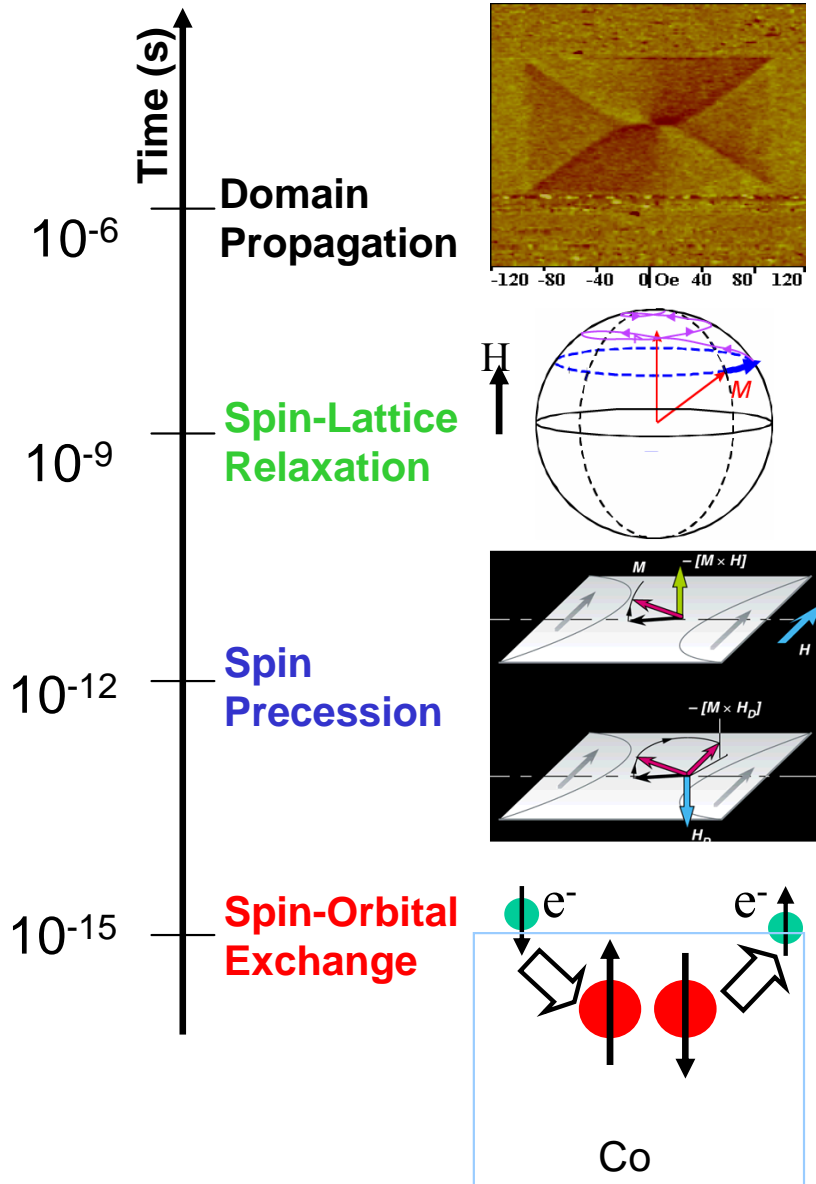
~100 ps (synchrotron)

Field: ~10 – 100 gauss (stripline)



# THz Driven Magnetic Dynamics

*Use ultra-short magnetic field pulses to induce spin excitations (D. Arena / NSLS)*

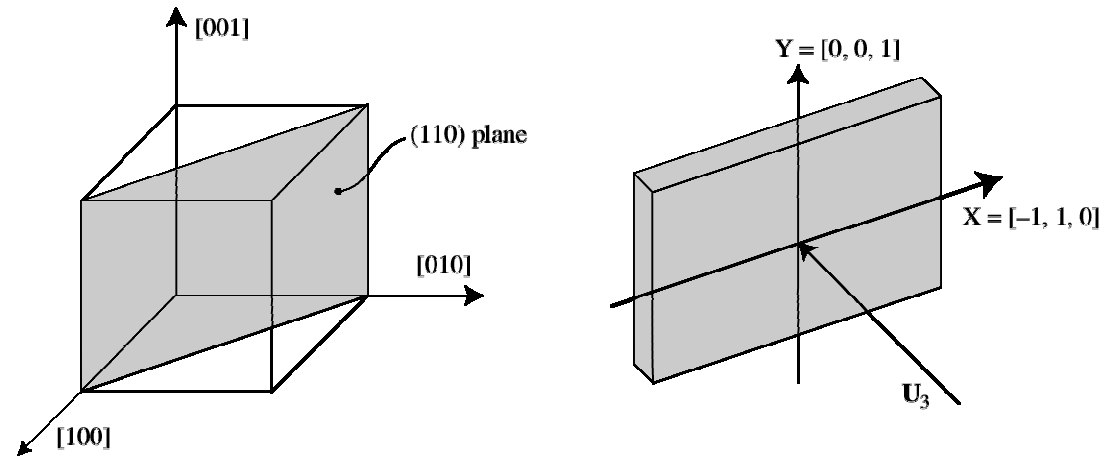


Excitation / Interaction	Timescale (sec)
Exchange interaction	10 <sup>-15</sup>
Stoner excitations	10 <sup>-15</sup> - 10 <sup>-14</sup>
Spin waves	10 <sup>-12</sup> (low q limit)
Spin - lattice relaxation	10 <sup>-12</sup> - 10 <sup>-11</sup> (in manganites)
Precessional motion	10 <sup>-10</sup> - 10 <sup>-9</sup>
Spin injection	TBD
Spin diffusion	TBD
Spin coherence	TBD

# Electro-Optic Details for ZnTe

S. Casalbuoni, H. Schlarb, B. Schmidt, P. Schmüser,  
B. Steffen, A. Winter *DESY & Universität Hamburg*

“Numerical Studies on the Electro-Optic Sampling of  
Relativistic Electron Bunches” (TESLA Report 2005-01)



$$\cos 2\psi = \frac{\sin \alpha}{\sqrt{1 + 3 \cos^2 \alpha}}$$

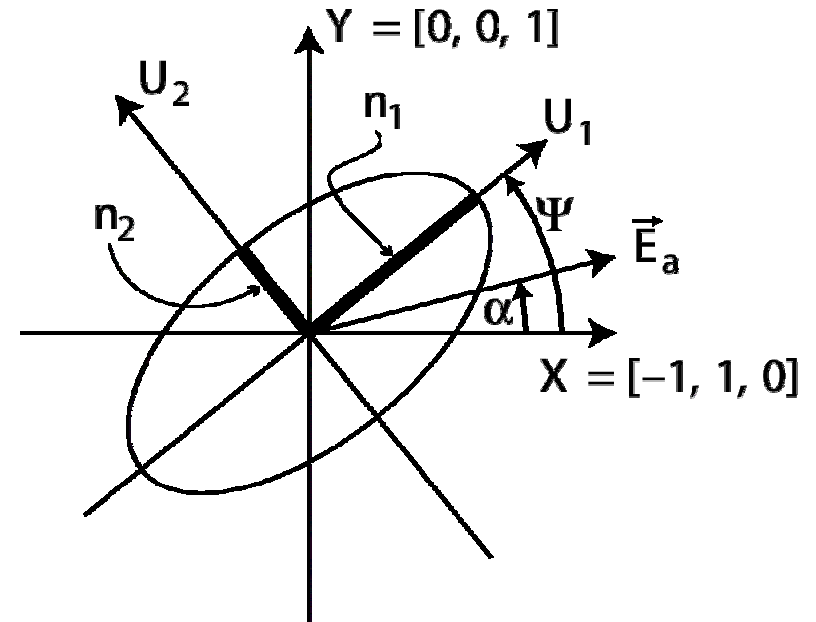
$$\alpha = 0 \rightarrow \psi = \pi/4 (45^\circ)$$

$$n_1 = n_0 + \frac{n_0^3 r_{41} E_a}{4} \left( \sin \alpha + \sqrt{1 + 3 \cos^2 \alpha} \right)$$

$$n_2 = n_0 + \frac{n_0^3 r_{41} E_a}{4} \left( \sin \alpha - \sqrt{1 + 3 \cos^2 \alpha} \right)$$

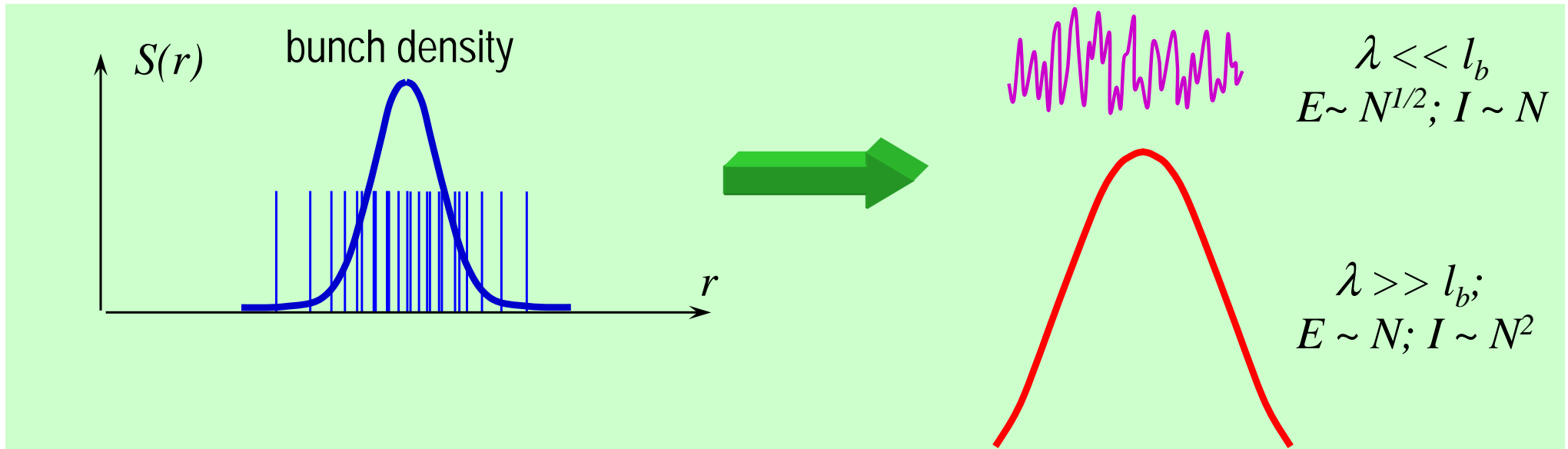
$$n_3 = n_0 - \frac{n_0^3 r_{41} E_a}{2} \sin \alpha .$$

$$\Delta\phi(E) = \frac{2\pi L}{\lambda_0} (n_1 - n_2) = \frac{2\pi L}{\lambda_0} \Delta n(E)$$



# Multi-particle Coherent Synchrotron Radiation (CSR)

Accelerators typically have many electrons traveling in a “bunch”. Can emission be coherent?  
Yes -- if bunch (or some portion of it) has length that is short compared to wavelength.



$$\frac{dI(\omega)}{d\omega} \underset{\text{multiparticle}}{=} [N + N(N-1)f(\omega)] \frac{dI(\omega)}{d\omega} \sim N^2$$

$$\text{where } f(\omega) = \left| \int_{-\infty}^{\infty} e^{i\omega \hat{n} \cdot \vec{r}/c} S(r) dr \right|^2 \quad (\text{Nodvick \& Saxon})$$

*In some accelerators, bunch lengths are 100s of fs ( $\Rightarrow$  THz), and  $N$  can be large e.g.  $\sim 10^{10}$*

## Keil-Schnell

(coasting / unbunched beam)

$$eI_{ave} \frac{Z_n}{n} \leq 2\pi\alpha E \sigma_E^2$$

→  $I_{th} \propto \alpha \sim f_{s0}^2$

## Boussard

replace  $I_{ave}$  with  $I_{peak}$

→  $I_{th} \propto \alpha^{3/2} \sim f_{s0}^3$

